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#### **Final Technical Report**

## IMPROVING THE ASSESSMENT OF SITE-SPECIFIC SEISMIC HAZARDS THROUGH THE LENS OF NOVEL ATTENUATION MODELS

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#### **Abstract**

Site-specific attenuation can be defined by means of the distance-independent spectral decay parameter  $\kappa_0$  (Anderson and Hough, 1984). However, estimates of  $\kappa_0$  are currently burdened with uncertainties including the ones associated with calculations at a single site, estimates beyond the linear-elastic elastic regime, and model-to-model variability. This report describes the work done under grant number G19AP00058, entitled "Improving the Assessment of Site-specific Seismic Hazards Through the Lens of Novel Attenuation Models" and it is presented in three parts.

**Part I** investigates the variability in kappa,  $\kappa$ , estimates at a single station (what we refer to as within-station variability). A better understanding of potential factors that lead to large scatter in estimated values of  $\kappa$  constitutes a critical need for ground motion modeling and seismic hazard assessment at large. Most research efforts to date have focused on studying the site-to-site variability of  $\kappa$ , but the uncertainties in individual  $\kappa$  estimations associated with different events at a selected site remain uncharacterized. This part is reproduced from an article written by the same authors (in collaboration with Drs. Fabrice Cotton, Marco Pilz, and Dino Bindi from the German Center of Geosciences at Potsdam, Germany) and published in the Bulletin of the Seismological Society of America (BSSA) in April 2020 (<a href="https://doi.org/10.1785/0120190253">https://doi.org/10.1785/0120190253</a>).

**Part II** aims to quantify near-surface attenuation (as captured by  $\kappa$ ) beyond the linear-elastic regime. Soil nonlinear behavior, often triggered in soft sedimentary deposits subjected to strong ground shaking has led to catastrophic damage to civil infrastructure in many past earthquakes. Nonlinear behavior in soils is associated with larger shear strains, increased material damping ratio and reduced stiffness. However, most investigations of the high-frequency spectral decay parameter  $\kappa$ , have focused on low-intensity ground motions inducing only small shear strains. Because studies of the applicability of  $\kappa$  when larger deformations are induced are rather limited, we investigate the behavior of  $\kappa$  (both, individual  $\kappa_r$  and site-specific  $\kappa_0$  estimates) beyond the linear-elastic regime. This second part of the completed work was submitted to the BSSA special section on Advances in Site Response and it was still under review by the time of publication of this final technical report. Dr. Luis Fabian Bonilla and Dr. Celine Gelis from IFSTTAR and IRSN, respectively, are co-authors of this portion of the study.

**Part III** explores model-to-model variability in  $\kappa$  values and provides recommendations for future research addressing limitations and challenges identified for the different approaches considered. Particularly, this study focuses on the challenges associated with the lack of data in low-to-moderate seismicity regions, which does not allow the use of the classical acceleration spectrum methodology to compute individual values of  $\kappa$  in the Fourier Amplitude Spectrum of multiple ground motion recordings. This part of the study was conducted in collaboration with Dr. Linda Al Atik, Dr. Abhinav Gupta and PhD student Sugandha Singh from NCSU.

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## Part I: Within-Station Variability in Kappa: Evidence of Directionality Effects

#### 1. Introduction

The characterization of attenuation at various scales (from regional to local) constitutes a critical component in the prediction of ground motions, site response analysis and seismic hazard assessments. Thus, understanding ground motion characteristics at high frequencies has become a research focus in recent studies (e.g., Mayor et al. 2018; Parolai 2018). The high-frequency decay parameter,  $\kappa$ , was proposed by Anderson and Hough (1984) to characterize linear decay of the shear-waves (S-wave) Fourier acceleration amplitude spectrum (FAS) in log-linear scale in the high-frequency range. In general, individual estimations of  $\kappa$  values, hereafter referred to as  $\kappa_r$ , are decomposed into a site-specific component,  $\kappa_0$ , a generalized distance-dependency component,  $\kappa_R$ , and a source component,  $\kappa_S$  (Ktenidou et al. 2014).

The site-specific component,  $\kappa_0$ , captures the attenuation taking place directly below the site of interest (Ktenidou et al. 2013), but further investigation is required to define the depth of the geologic profile that contributes toward the  $\kappa_0$  resulting at the ground surface. Ground motion models and their adjustments from host to target regions have used estimates of  $\kappa_0$  to characterize the effects of high frequency attenuation (e.g., Van Houtte et al. 2011, Campbell 2003, Ktenidou et al. 2014). Moreover, knowledge of  $\kappa_0$  benefits the identification of epistemic uncertainties to remove the ergodic assumption in site-specific probabilistic seismic hazard analysis (PSHA), which is crucial for the seismic design of critical facilities such as nuclear power plants (Rodriguez-Marek et al. 2014, Cabas and Rodriguez-Marek 2017). Deciphering the physics behind empirical estimates of  $\kappa_0$  requires understanding the site's contribution to the overall attenuation. Decoupling local and regional attenuation mechanisms will facilitate the development of physics-based ground motion simulations and non-ergodic ground motion prediction equations (GMPEs).

Previous studies have investigated the correlation between  $\kappa_0$  and other site parameters, such as the time-averaged shear-wave velocity of the top 30 m subsoil (V<sub>s30</sub>) (e.g., Van Houtte et al. 2011, 2014, Ktenidou et al. 2015, Cabas et al. 2017), but large uncertainties in  $\kappa_r$  estimations (which also affect the computation of  $\kappa_0$ ) impose difficulties to unveil the physical meaning of  $\kappa_0$  (Perron et al. 2017). An understanding of the sources of variability affecting  $\kappa_r$  and  $\kappa_0$  constitutes a crucial step toward robust and sustainable applications of  $\kappa_0$  in earthquake engineering practice.

The variability of  $\kappa$  has been studied through different lenses in the last decade, from model-to-model variability (e.g., Ktenidou et al. 2014, Edwards et al. 2015, Perron et al. 2017), user-to-user variability (e.g., Edwards et al. 2015, Douglas et al. 2010), to site-to-site variability (e.g., Van Houtte et al. 2011, 2014, Cabas et al. 2017). Some have investigated the variability in  $\kappa_r$  and  $\kappa_0$  estimates when utilizing a single methodology, but incorporating alternative assumptions throughout the implementation (e.g., Ktenidou et al. 2013). Other efforts have focused on understanding the correlation (or lack thereof) among different methods to obtain  $\kappa_0$  (e.g.,

Ktenidou et al. 2014, Perron et al. 2017). Whilst, the variability of  $\kappa_0$  as a function of site conditions have been extensively studied for multiple regions, including Japan, Greece, France and the US (e.g., Douglas et al. 2010, Laurendeau et al. 2013, Ktenidou et al. 2015, Cabas et al. 2017, Parolai 2018).

The objective of this study is to characterize the within-station variability of  $\kappa_0$ . Ten stations from the Japanese database, KiK-net, are investigated. Their corresponding National Earthquake Hazards Reduction Program (NEHRP) site class classification varies from B (rock) to D (stiff soils). First, we introduce a framework to evaluate aleatory variability and epistemic uncertainty in  $\kappa_r$  and  $\kappa_0$ . Then, we focus on individual values of  $\kappa_r$  calculated following the traditional approach by Anderson and Hough (1984) at the ten study sites, and investigate how ground motion directionality affects the estimation of  $\kappa_r$ . Finally, we explore the influence of earthquake type and focal depth on the estimates of  $\kappa_R$  and  $\kappa_0$ . Within one selected station, we find that values of  $\kappa_R$  and  $\kappa_0$  are affected by repeatable contributions from the path, with these path effects being more significant for  $\kappa_R$ .

#### 2. Uncertainty and Variability in Kappa

Empirical data from multiple seismic events and recording stations are used to construct ground motion models (GMM) that can describe the distribution of ground motion in terms of a median and a logarithmic standard deviation,  $\sigma$  (Al Atik et al. 2010). The aleatory variability in the ground motion, represented by  $\sigma$  has proven to exert a strong influence on hazard estimates, especially at low annual exceedance frequencies (Bommer and Abrahamson 2006, Al Atik et al., 2010, Rodriguez-Marek et al., 2014). Defensible reductions in  $\sigma$  are desirable not only because of their ultimate effect on PSHA, but also because they result from a clear separation of aleatory variability (which is theoretically irreducible) and epistemic uncertainty (which can be reduced with the collection of new data, Rodriguez-Marek et al. 2014). In pursuit of defensible reductions in  $\sigma$ , repeatable source, path, and/or site contributions can be identified at a single site and invoke the nonergodic assumption. The ergodic assumption implies that the temporal distribution of ground motions at a given site is equivalent to the spatial distribution of ground motions across many sites (given the same causal parameters, Kuehn et al. 2019).

In this study, we focus on identifying repeatable site and path contributions to the observed variability in  $\kappa_r$ ,  $\kappa_R$  and  $\kappa_0$ . Drawing parallels to the residual analysis process in ground motion modeling, this work aims to provide a characterization of the within-station variability in  $\kappa_r$  and  $\kappa_0$  estimates, which can further support the development of the site-term parameterization in nonergodic GMMs. Baltay et al. (2017) provided evidence of a correlation between  $\kappa_0$  values and the average site residual, using small-magnitude ground motion data recorded at ten stations from the ANZA network. Estimates of  $\kappa_0$  could inform predictions of station-specific site residuals in partially nonergodic GMMs "to improve our physical understanding of the site term at specific stations" (Baltay et al. 2017). We select a subset of recordings at selected stations from the KiKnet database to identify and quantify systematic, repeatable contributions to  $\kappa_r$ ,  $\kappa_R$  and  $\kappa_0$  estimates; hereafter referred to as within-station variability in  $\kappa$ .

Approaches to estimate  $\kappa_0$  can be classified into two types, namely direct estimates and empirical estimates from statistical regressions. Factors that introduce variability in  $\kappa_0$  estimates for each type are grouped into six categories with considerations of model selections, database choices and record processing protocols as shown in **Figure 1**. The latter provides a framework to investigate epistemic uncertainties in  $\kappa_0$  estimates for the linear elastic regime only. Further research is required should soil nonlinearity be triggered. The description of each category depicted in **Figure 1** is presented below.

#### • Part 1 $\kappa_0$ -model

The commonly used statistical regression approach is based on a linear distance-dependent model, where  $\kappa_0$  represents the site-specific component, while  $\kappa_R$  refers to the regional attenuation. Values of  $\kappa_0$  and  $\kappa_R$  are obtained via empirical linear regression of  $\kappa_r$  following the Anderson and Hough (1984) method. Alternatively, direct estimates of  $\kappa_0$  can be obtained from the site properties (e.g., measurements of  $\kappa_0$  in the high frequency decay of a transfer function, Drouet et al. 2010) without the definition of the  $\kappa_0$ - linear regression model. The choice of a linear regression as opposed to other possible functional forms has been mostly based on the simplicity of the model and observed fit to the empirical data (Ktenidou et al 2013).

#### • Part 2 depth-dependency

The measured  $\kappa_0$  values can be depth-dependent or thickness–dependent based on the approach selected for the respective calculations. Values of  $\kappa_0$  provide an estimate of attenuation directly below the depth at which the ground motions are recorded. Different  $\kappa_0$  values are typically obtained at different depths within a site profile (e.g., Ktenidou et al 2015). Values of site-specific  $\kappa_0$  have also been proposed to represent the contribution of a specific soil column with a given thickness (e.g., Campbell 2009).

#### • Part 3 approach choice

Previous studies show that various kappa calculation approaches will result in different individual  $\kappa_r$  values (for the same ground motion), and ultimately different  $\kappa_0$  estimates (e.g., Ktenidou et al 2014). Understanding the suitability of each method in consideration of the available records and site conditions is relevant to reduce uncertainties in kappa estimations. In Figure 1,  $\kappa_{r_-BB}$ ,  $\kappa_{r_-DS}$  and  $\kappa_{r_-AS}$  refer to individual values of kappa from the broadband method (Ktenidou et al., 2016), the displacement method (Biasi and Smith, 2001), and the acceleration spectrum method (Anderson and Hough 1984), respectively. Direct measurement approaches also shown in Figure 1 include estimations of  $\kappa_0$  from the response spectrum,  $\kappa_{0\_RESP}$  (Silva and Darragh 1995), utilizing inverse random vibration theory,  $\kappa_{0\_IRVT}$  (Al Atik et al 2014), and from the site's transfer function,  $\kappa_{0\_TF}$  (Drouet et al 2010).

#### Part 4 dataset choice

Choosing an appropriate dataset can reduce the within-station variability in  $\kappa_0$  by constraining the uncertainties associated with individual  $\kappa_r$  values. In general, only magnitude, source-to-site distance, and type of seismicity are used to select appropriate ground motions for kappa calculations. However, we hypothesize that considering the events' azimuth, and focal depths can provide insights on other sources of within-station variability.

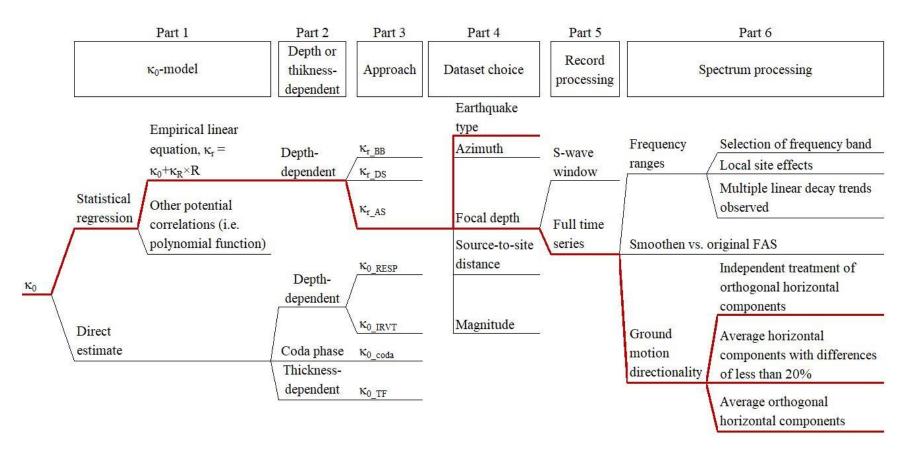
#### Part 5 record processing

The variability associated with record processing refers to differences stemming from the usage of the S-wave window or the whole time series to calculate  $\kappa_r$  values. Anderson and Hough (1984) originally introduced the calculation of  $\kappa_{r\_AS}$  as the linear decay of the S-wave FAS in the high frequency range. However, varying selections of the S-wave window can introduce additional scatter in  $\kappa_r$  for the same event (Douglas et al. 2010, Cabas et al. 2017, Xu et al. 2019). This additional variability may be caused by the assumed duration of the selected S-wave window or by the explicit consideration of the direct S-wave only or the direct S-wave window and coda/surface waves. Values of  $\kappa_{r\_AS}$  estimated from the S-wave window could be significantly biased by scattering effects, except when intrinsic attenuation is dominant (Parolai et al. 2015, Pilz and Fah 2017, Parolai 2018, Pilz et al. 2019).

#### • Part 6 spectrum processing

The estimation of  $\kappa_{r\_AS}$  is significantly sensitive to the selection of frequency ranges, including: (1) the length of the frequency band; (2) local site conditions such as site-amplification peaks (Parolai and Bindi 2004); and (3) the presence of multiple linear decay trends in the high frequency range of the FAS. Using smoothen FAS instead of the original FAS also introduces differences for  $\kappa_r$  estimates. Additionally, there is variability resulting from different approaches to treat recorded horizontal components. For instance, (a) treating orthogonal horizontal components independently (Dimitriu et al. 2001), (b) averaging  $\kappa_{r\_AS}$  values estimated from as-recorded horizontal components if differences in these  $\kappa_{r\_AS}$  values are less than 20% (Ktenidou et al. 2013), and (c) averaging  $\kappa_{r\_AS}$  values estimated from as-recorded horizontal components without consideration of the corresponding differences in individual  $\kappa_{r\_AS}$ .

We would like to emphasize that the ultimate influence of the aforementioned sources of variability is usually station-dependent, although the logic tree and framework described in **Figure 1** can be implemented at any site. Thus, the significance of each branch is unique for a given site, which results in a better characterization of the within-station variability at the site. In this paper, we only focus on the branches highlighted in **Figure 1**. The Anderson and Hough (1984) method is used to investigate systematic contributions to the variability in  $\kappa_r$  (hereafter referred to as  $\kappa_{r\_AS}$ ) and  $\kappa_0$ . We investigate the within-station variability caused by (1) the dataset choice (part 4) based on earthquake types and focal depths, and (2) spectrum processing (part 6) by understanding the contributions of ground motion directionality.

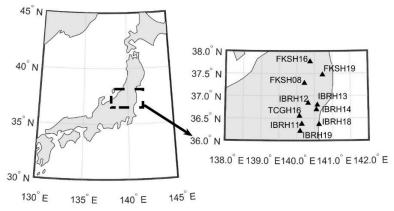


**Figure 1.** Logic tree for the estimation of  $\kappa_0$  values. The highlighted branches are explored in this work.

#### 3. Database Description and Study sites

We use the Japanese Kiban-Kyoshin network (KiK-net) database (see Data and Resources Section), which is a strong-motion seismograph network uniformly deployed at more than 600 locations in Japan and able to provide high-quality data at various site classes. KiK-net has a pair of seismographs at each station, one located on the ground surface, and the other one in a borehole together with high-sensitivity (Hi-net) seismographs. The depth of each borehole sensor is typically between 100 m and 200 m. Instrumental sampling frequencies are 100 Hz or 200 Hz. Wave velocity profiles (for both P-wave and S-wave) at each station are measured by downhole PS logging, and the corresponding files are available on the KiK-net website (see Data and Resources). The orientations of orthogonal ground surface sensors are north-south and east-west. However, difficulties during installation and regular maintenance at some stations may have changed the orientations of borehole sensors (Aoi et al. 2004, Aoi et al. 2011). The azimuths of borehole sensors at each KiK-net station are available on the Hi-net website (see Data and Resources). The entire dataset and flatfile used in this paper is built and compiled with an automated protocol by Dawood et al. (2016). The seismic moment magnitude M<sub>w</sub>, focal depth, epicenter location and focal mechanism information are obtained from the NIED moment tensor solution available at the broadband seismography network (F-net) catalogue.

In this paper, recorded horizontal components at the ground surface and at depth are used. The criteria for selection of ground motions and stations include: (1) epicentral distances less than 150 km; (2)  $M_w$  larger than 4.0; (3) peak ground acceleration (PGA) values at the surface less than 0.01 g (to avoid effects of soil nonlinearity); (4) at least 50 available records complying with requirements (1) to (3) per study site; (5) the signal-to-noise ratio (SNR) larger 3.0 over the frequency ranges for  $\kappa_{r\_AS}$  estimation. Moreover, the ability of shear-wave velocity profiles measured by downhole logging at KiK-net stations to describe actual site conditions has been questioned in the past (Wu et al. 2017). 2D/3D wave propagation could be significant at some KiK-Net stations because of the edge-generated surface waves, topographic effects and focusing effects. However, the potential for site scattering effects can be reduced as we considered KiK-Net sites with reliable shear wave velocity (V<sub>s</sub>) profiles that meet the 1D wave propagation assumptions based on the results from Pilz and Cotton (2019). Thus, ten stations corresponding to various site classes (NEHRP site class from B to D) are selected in this study. Key characteristics pertaining these study sites are provided in **Figure 2** and **Table 1**.



**Figure 2.** Locations of each selected Japanese station in this study.

**Table 1**. Selected stations information.

Station Name	Station Latitude	Station Longitude	$^*V_{s30}$	<sup>†</sup> Hole Depth	††H <sub>800</sub>	Borehole Sensor Azimuth	§NEHRP Site
	degree	degree	m/s	m	m	degree	— Class
FKSH08	37.28	140.22	562.50	105	8	-3	С
FKSH16	37.76	140.38	531.61	300	180	1	C
FKSH19	37.47	140.73	338.06	100	20	-4	D
IBRH11	36.37	140.14	242.49	103	30	0	D
IBRH12	36.83	140.32	485.71	200	20	-3	C
IBRH13	36.79	140.58	335.37	100	34	2	D
IBRH14	36.69	140.55	829.12	100	10	-1	В
IBRH18	36.36	140.62	558.56	504	30	0	C
IBRH19	36.21	140.09	692.31	210	2	-1	C
TCGH16	36.54	140.08	213.20	112	NaN	-2	D

<sup>\*</sup>V<sub>s30</sub>: the time-averaged shear-wave velocity of the top 30 m subsoil

#### 4. Methods

#### 4.1. Estimation of $\kappa_r$ and $\kappa_0$

We use the acceleration spectrum approach (Anderson and Hough, 1984) to estimate  $\kappa_{r\_AS}$ . The slope of the linear decay,  $-\pi\kappa_{r\_AS}$ , of the acceleration FAS in the high frequency range using log-linear coordinates is calculated for each horizontal component of the selected records. A weighted robust least square linear regression with Bisquare function over a manually selected high-frequency range ( $[f_1, f_2]$ ) (see **Figure 3** as an example). The minimum difference between  $f_1$  and  $f_2$  is 8 Hz. Following the recommendations of Ktenidou et al. (2013),  $f_1$  is larger than the corresponding earthquake source-corner frequency ( $f_c$ ), computed by Equation (1) (Brune, 1970, 1971):

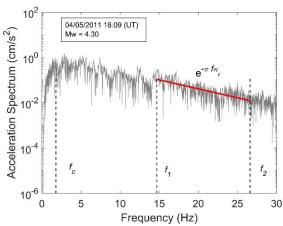
$$f_c = 4.9 \times 10^4 \beta \left(\frac{\Delta \sigma}{M_0}\right)^{\frac{1}{3}} \tag{1}$$

Where  $f_c$  is in Hz,  $\beta$  is the shear-wave velocity near the source with units of km/s,  $\Delta \sigma$  is the stress drop in MPa, and  $M_0$  is the seismic moment in N·m. In this article,  $\beta$  is assumed to be 3.6 km/s (Pei et al. 2009). The value of  $\Delta \sigma$  is assumed to be 3 MPa for crustal earthquakes and 5.5 MPa for subduction zone events (Nakano et al. 2015). Moreover, because the instrument's response is approximately flat below 30 Hz (which is close to the response of a three-pole Butterworth filter with a cutoff frequency of 30 Hz), we restrict  $f_2$  to be less than 30 Hz (Aoi et al. 2004, Fujiwara et al. 2004, Oth et al. 2011, Laurendeau et al. 2013, Cabas et al. 2017).

<sup>†</sup>Hole-depth: the depth of borehole sensor relative to the ground surface

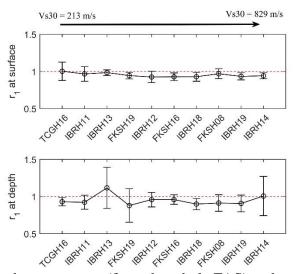
<sup>††</sup>H<sub>800</sub>: depth to a horizon with velocity V<sub>s</sub> of 800 m/s or more

<sup>§</sup>NEHRP Site Class: National Earthquake Hazards Reduction Program (NEHRP) site class classification



**Figure 3.** Selection of  $f_1$  and  $f_2$  on the Fourier acceleration amplitude spectrum corresponding to a surface record at station IBRH20.  $f_c$  refers to the corner frequency as estimated by the Brune (1970) model with stress drop of 3.0 MPa for active crustal events.

The S-wave window is often used to estimate  $\kappa_{r}$  AS. Previous studies have picked the direct Swave manually assuming a minimum duration of 5 sec for small/nearby events and 20 sec for large/far events (Ktenidou et al. 2013). Whilst, others have included the coda wave within the selected S-wave window for records where the coda wave cannot be separated clearly (Anderson and Hough 1984). Differences in  $\kappa_{r,AS}$  (computed by the acceleration spectrum approach using the whole time series) and  $\kappa_{r}$  AS SW (computed by the acceleration spectrum approach using manually selected S-wave windows, following Anderson and Hough (1984)) are compared for records from shallow crustal earthquakes used in this study (see **Figure 4**). The same frequency range,  $f_1$  and  $f_2$ , is applied to each record to avoid bias from frequency range selections. The ratio,  $r_1$  =  $\kappa_{r}$  AS/ $\kappa_{r}$  AS sw, is computed at each study site to represent the differences between  $\kappa_{r}$  AS and  $\kappa_{r}$  AS SW in **Figure 4**. Values of  $\kappa_{r}$  AS SW are generally larger than  $\kappa_{r}$  AS at the study sites (i.e.,  $r_{1}$  is generally less than 1.0). Scattering effects can help explain observed lower  $\kappa_{r\_AS}$  values from the whole time series. When intrinsic attenuation is strong at a given site, higher frequencies can be removed more efficiently resulting in a steep slope in the S-wave FAS (Parolai et al. 2015). The full time series is composed of the direct S-waves, but also scattered waves from the redistribution of the seismic waves' energy. The latter can modify the slope in the FAS at high frequencies producing a biasedk<sub>r\_AS</sub>, which generally is lower. Moreover, the S-wave window dominates the spectrum at surface and the downgoing waves could more affect the borehole time series. Thus, more variations between  $\kappa_{r\_AS}$  and  $\kappa_{r\_AS\_SW}$  at depth are observed. Because the differences between  $\kappa_{r\_AS\_SW}$  and  $\kappa_{r\_AS}$  are less than 20% for most of the selected ground motions used in this study, we choose the full time series to estimate  $\kappa_{r\_AS}$  values. Further guidance in the selection of the Swave window for kappa calculations can provide meaningful insights to reduce the betweenstation variability in kappa.



**Figure 4.** Comparison between  $\kappa_{r\_AS}$  (from the whole FAS) and  $\kappa_{r\_AS\_SW}$  (from the S-wave window FAS) corresponding to our ten study sites.  $r_1$  is the ratio computed by  $\kappa_{r\_AS}/\kappa_{r\_AS\_SW}$ . The dash line represents a ratio of 1.0. The circles depict the mean  $r_1$  of all observed records, and the error bars indicate the +/- standard derivation of all observed ratios at each site of interest.

We choose the linear  $\kappa_0$ -model introduced by Anderson (1991) and follow the nomenclature proposed by Ktenidou et al. (2013) to estimate the site component  $\kappa_0$ :

$$\kappa_{r\_AS} = \kappa_0 + \kappa_R \cdot R_{epic} \tag{2}$$

Where the  $\kappa_{r,AS}$ , and  $\kappa_0$  are expressed in units of time (s),  $\kappa_R$  in units of s/km, and  $R_{epic}$  is the epicentral distance in km. This κ<sub>0</sub>-model assumes a unique source-to-site path for each record, and a homogeneous, frequency-independent seismic quality factor, Q (Knopoff 1964). Thus, we only select events with epicentral distances less than 150 km to minimize the potential for multiple source-to-site ray paths per record. The assumption of a unique Q-value allows for the calculation of  $\kappa_R$  (following the linear model in Equation (2)), which describes regional attenuation. Japan has varying Q-values across the region, with lower Q-values in the central Japanese island and higher Q-values on the east coast (Pei et al. 2009, Nakano et al. 2015). The low Q- and high Q-value regions are separated by Japan's volcanic belt. Thus, we avoid using records that cross the volcanic belt during their propagation path from source to site based on the attenuation classification map provided by Nakano et al. (2015). The  $\kappa_0$ -model in Equation (2) is also based on the assumption that the source contribution is negligible (Ktenidou et al. 2014, Van Houtte et al. 2011). For the selected KiK-net stations, the path component,  $\kappa_R$ , is constrained to be the same for both surface and borehole records because the regional attenuation contributions should be identical when analyzing individual stations (Ktenidou et al. 2013, 2015, Cabas et al. 2017). We use the maximum likelihood method to model  $\kappa_r$  AS with the constrained  $\kappa_R$  based on Equation (2).

#### 4.2. Ground Motion Directionality

A recorded ground motion at a specific site can vary depending on sensor orientation (Boore et al. 2006). This lack of uniformity of ground motions in all possible orientations is known as ground

motion directionality. Two as-recorded horizontal orthogonal components of each selected ground motion are rotated to study the influence of ground motion directionality on the estimation of  $\kappa_{r\_AS}$ . All records are rotated using the following equations (Boore et al. 2006, Boore 2010):

$$a_{ROT-1}(t;\theta) = a_1(t)\cos(\theta) + a_2(t)\sin(\theta)$$
(3)

$$a_{ROT-2}(t;\theta) = -a_1(t)\sin(\theta) + a_2(t)\cos(\theta)$$
(4)

Where  $a_1(t)$  and  $a_2(t)$  are the as-recorded acceleration time series,  $a_{ROT_{-1}}(t;\theta)$  and  $a_{ROT_{-2}}(t;\theta)$  are the rotated motions with the corresponding rotation angle  $\theta$ . The  $\kappa_{r,AS}$  values computed from the corresponding FAS of rotated motions are referred to as  $\kappa_{r,AS,ROT}$ . In this article, we only rotate one single horizontal component  $(a_1(t) \text{ or } a_2(t))$  from  $0^{\circ}$  to  $180^{\circ}$  (i.e., non-redundant angles) with increments of  $10^{\circ}$  to investigate the influence of ground motion directionality on  $\kappa_{r,AS}$ .

Considering that the frequency range ( $[f_1, f_2]$ ) to estimate  $\kappa_{r\_AS}$  is selected visually for each event, a large number of calculations is required for  $\kappa_{r\_AS\_ROT}$  estimations. Thus, we propose a semi-automatic algorithm to compute  $\kappa_{r\_AS\_ROT}$ . First, we select the frequency range based on visual inspection of the as-recorded motion from a given event (at a given site). Then, a common frequency range is selected for the pair of recorded horizontal components and applied to all the corresponding rotated motions from that same event at that station. The main advantage of the proposed procedure, beyond the optimization of the computational process, is that it avoids the introduction of additional uncertainties stemming from the frequency range selection. The performance of the proposed semi-automatic algorithm is evaluated by visually inspecting the rotated FAS plots and the corresponding frequency range.

The influence of ground motion directionality on the attenuation contributed by the soil column, hereafter referred to as  $\Delta\kappa(\theta)$ , is also investigated.  $\Delta\kappa(\theta)$  is calculated as follows, assuming the  $\kappa_R$  value remains unchanged:

$$\Delta \kappa(\theta) = \kappa_{r\_AS\_ROT\_sur}(\theta) - \kappa_{r\_AS\_ROT\_bore}(\theta)$$

$$= (\kappa_{0\_ROT\_sur}(\theta) + \kappa_R \times R_{epic}) - (\kappa_{0\_ROT\_bore}(\theta) + \kappa_R \times R_{epic})$$

$$= \Delta \kappa_{0\_ROT}(\theta)$$
(5)

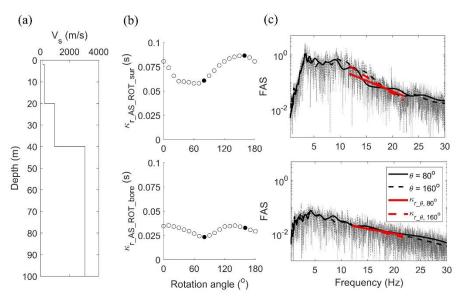
It should be noted that errors in the azimuth of borehole sensors (i.e., sensors not oriented in the true NS or EW directions) could propagate through the estimation of  $\Delta\kappa(\theta)$ , which means that values of  $\theta$  at the surface and at depth may not be consistent. The errors in the azimuth are observed at eight selected sites, and the maximum borehole sensor deflection is  $4^{\circ}$  (shown in Table 1). Thus, we correct the borehole record orientation with the azimuth of borehole sensors provided by Hinet before the borehole horizontal component is rotated.

#### 5. Results and Discussion

#### 5.1. Directionality effects on $\kappa_r$ and $\kappa_0$ estimations

A variation of  $\kappa_{r\_AS\_ROT}$  with rotation angle is observed for both surface and borehole records at all stations. **Figure 5** presents an example of the relationship between  $\kappa_{r\_AS\_ROT}$  and rotation angles at FKSH19. The corresponding FAS of the rotated components are also presented (i.e., with rotation angle of  $80^{\circ}$  and  $160^{\circ}$ ) for comparison purposes, depicting changes of the decay in the high-frequency range. The standard derivations corresponding to  $\kappa_{r\_AS\_ROT\_sur}$ , and  $\kappa_{r\_AS\_ROT\_bore}$  are 0. 0109 s and 0.0041 s, respectively.

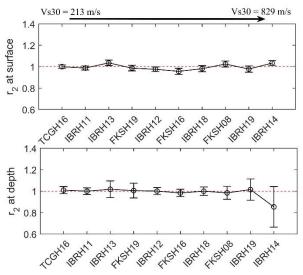
Figure 5 illustrates that the variation of  $\kappa_{r\_AS\_ROT}$  at the surface is more significant than at depth, which is also observed for the majority of records across all stations. We then investigate the influence of the event azimuth on the maximum  $\kappa_{r\_AS\_ROT}$  observed and its corresponding rotation angle. The rotation angle associated with the maximum  $\kappa_{r\_AS\_ROT}$  is hereafter referred to as  $\theta_{max}$ . A correlation between  $\theta_{max}$  and the azimuth of each record at the surface and at depth is not found.



**Figure 5.** Example of  $\kappa_{r\_AS\_ROT}$  variations. (a) Shear wave velocity profile at FKSH19, (b) comparison between  $\kappa_{r\_AS\_ROT}$  and rotation angle at surface and borehole for one record, and (c) the FAS for rotated components with  $\theta$  of  $80^{\circ}$  and  $160^{\circ}$ . The dark solid and dash lines show the smoothen FAS to emphasize the differences between rotated FASs. The select ground motion was a shallow active crustal event recorded at FKSH19 (site class: D) with seismic moment magnitude of 4.4, azimuth of  $19^{\circ}$ , and epicentral distance of 117 km (recorded on 07/26/2003 (UT)).

The mean of all  $\kappa_{r\_AS\_ROT}$  for each record,  $\kappa_{r\_AS\_mean}$ , and the average of  $\kappa_{r\_AS\_H1}$  and  $\kappa_{r\_AS\_H2}$  from the corresponding as-recorded horizontal components,  $\kappa_{r\_AS\_ave}$ , are compared in **Figure 6** by means of the ratio,  $r_2 = \kappa_{r\_AS\_ave} / \kappa_{r\_AS\_mean}$ . **Figure 6** demonstrates that the differences between  $\kappa_{r\_AS\_mean}$  and  $\kappa_{r\_AS\_ave}$  values at the ground surface are small; the maximum average of surface  $r_2$  across the ten study sites is 1.04 (at IBRH13;  $V_{s30} = 335$  m/s) and the minimum average is 0.96 (at FKSH16;  $V_{s30} = 532$  m/s). However, at station IBRH14 ( $V_{s30} = 829$  m/s), the differences of borehole  $\kappa_{r\_AS\_mean}$  and  $\kappa_{r\_AS\_ave}$  values are relatively large, with an average  $r_2$  of 0.85 and a standard derivation of  $r_2$  equal to 0.19. A closer inspection of the empirical transfer function (ETF)

at this station reveals that  $\kappa_{r\_AS}$  estimates at IBRH14 could be affected by the site-amplification in high frequencies, which can help explain observed differences between  $\kappa_{r\_AS\_mean}$  and  $\kappa_{r\_AS\_ave}$ . The corresponding ETFs at IBRH13, FKSH08, FKSH16, and FKSH19 also show varying site-amplification in the high frequency range. Considering the similarity observed between values of  $\kappa_{r\_AS\_mean}$  and  $\kappa_{r\_AS\_ave}$  for multiple ground motions and across study sites, an orientation-independent  $\kappa_r$  value for one recorded event at a given station can be estimated from the average of  $\kappa_{r\_AS\_H1}$  and  $\kappa_{r\_AS\_H2}$  computed from as-recorded orthogonal horizontal components directly. In the following sections, we use  $\kappa_{r\_AS\_ave}$  (also denoted as  $\kappa_{r\_AS}$  for simplicity) as the representative value for each pair of orthogonal horizontal components.



**Figure 6.** Comparison between mean  $\kappa_{r\_AS}$  of rotated motions (i.e.,  $\kappa_{r\_AS\_mean}$ ) and mean  $\kappa_{r\_AS}$  of two recorded horizontal component (i.e.,  $\kappa_{r\_AS\_ave}$ ) at selected stations along with the corresponding standard derivation at (a) borehole and (b) ground surface.  $r_2$  corresponds to the ratio  $\kappa_{r\_AS\_ave}/\kappa_{r\_AS\_mean}$ . The dash line indicates an  $r_2$  equal to 1.0, and the circles depict the mean  $r_2$  across all records considered per station. The error bars indicate the +/- standard deviation of all  $r_2$  computed at each site of interest.

The effects of ground motion directionality on  $\Delta\kappa(\theta)$  (Equation (5)) are also explored to investigate how the orientation of ground motion can affect the seismic attenuation taking place throughout the soil column. **Figure 7** and **Table** 2 show the variations of  $\Delta\kappa(\theta)$  at the sites of interest. First, we observe that the seismic attenuation contributed by the soil column is affected by ground motion directionality. Second, there seems to be a systematic variation with directionality unique to each site, with the maximum  $\Delta\kappa(\theta)$  generally corresponding to the same rotation angle across different ground motions at each station. Kotha et al. (2019) proved that the contribution of radiation pattern to the ground shaking characteristics would be weak and random in the high frequency range. Thus, we hypothesize that the influence of ground motion directionality on the high-frequency parameter  $\kappa$  is station-dependent and not affected by the earthquake source. Moreover, the maximum  $\sigma$  for  $\Delta\kappa(\theta)$  is observed at FKSH16, which has a thick soil column (holedepth of 300 m, and  $H_{800} = 180$  m) and a  $V_{s30} = 532$  m/s. The minimum  $\sigma$  value is found at IBRH19 with  $H_{800}$  or  $V_{s30}$  or 692 m/s and hole-depth of 210 m. However, a strong correlation between  $\sigma$  and  $H_{800}$  or  $V_{s30}$  or hole depth is not evident across all study sites. Different site parameters (or

a combination of existing ones) with considerations of shallow and deeper geologic structures are required to further detect potential correlations between site conditions and variability in  $\Delta \kappa_0$  due to ground motion directionality.

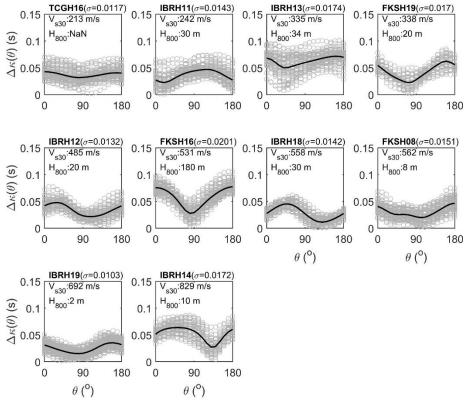


Figure 7. Variability of  $\Delta\kappa(\theta)$  at the stations of interest and the corresponding site information. The solid lines represent the mean of all  $\Delta\kappa(\theta)$  across all records per rotation angle, while the gray circles depict  $\Delta\kappa(\theta)$  obtained for each record and multiple rotation angles. H<sub>800</sub> refers to depth to a horizon with velocity  $V_s$  of 800 m/s or more.

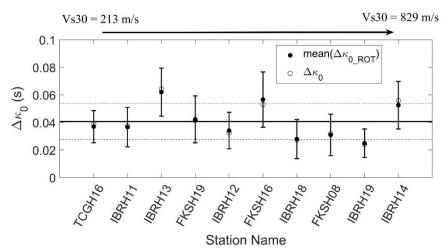
Finally, we compare the mean of all  $\Delta\kappa(\theta)$  values with the difference between surface and borehole  $\kappa_0$  values (hereafter referred to as  $\Delta\kappa_0$ ) from empirical linear regressions conducted on as-recorded horizontal components (i.e., averaging as-recorded  $\kappa_{r\_AS}$  values for each pair) at each station (**Figure 8**). Mean values of  $\Delta\kappa(\theta)$  shown in **Figure 8** are only slightly higher than the corresponding  $\Delta\kappa_0$  values, which indicates that the mean of two as-recorded  $\kappa_{r\_AS}$  values can lead to an orientation-independent estimation of  $\Delta\kappa_0$ . **Figure 8** also provides a comparison of the within-station and between-station variability of  $\Delta\kappa(\theta)$ . For most stations considered in this study (i.e., FKSH08, IBRH14, IBRH12, FKSH19, IBRH18, IBRH13 and IBRH11), the within-station variability in  $\Delta\kappa(\theta)$  is comparable and sometimes more significant, which evidences the need for a more rigorous consideration of the within-station variability in  $\kappa_0$  estimates. We note that the observed larger within-station variabilities in  $\Delta\kappa(\theta)$  at IBRH13, IBRH14, FKSH08, and FKSH19 can be influenced by site-amplification effects at these sites in the high frequency. The latter can induce bias in the resulting  $\kappa$  values. The quantification of the within-station variability in  $\kappa$  will result in more reliable  $\kappa_0$  estimates, which can inform empirical correlations with local site conditions.

**Table 2.** Station information and statistical parameters for  $\Delta \kappa(\theta)$ 

Station Name	*Hole Depth	†H <sub>800</sub>	$^{\dagger\dagger}V_{s,mean}$	$^{\S}\sigma(\Delta\kappa(\theta))$	$^{\parallel}$ mean( $\Delta \kappa(\theta)$ )	**NEHRP Site Class
	m	m	m/s	S	S	
IBRH14	100	10	1601.44	0.0172	0.0525	В
IBRH19	210	2	1792.68	0.0103	0.0249	C
FKSH08	105	8	936.59	0.0151	0.0310	C
IBRH18	504	30	1522.67	0.0142	0.0279	C
FKSH16	300	180	841.95	0.0201	0.0566	C
IBRH12	200	20	967.53	0.0132	0.0341	C
FKSH19	100	20	842.76	0.0170	0.0422	D
IBRH13	100	34	793.95	0.0174	0.0620	D
IBRH11	103	30	649.92	0.0143	0.0366	D
TCGH16	112	NaN	369.34	0.0138	0.0369	D

<sup>\*</sup>Hole-depth: the depth of borehole sensor relative to the ground surface

<sup>\*\*</sup>NEHRP Site Class: National Earthquake Hazards Reduction Program (NEHRP) site class classification



**Figure 8.** Comparison of mean( $\Delta \kappa(\theta)$ ) and  $\Delta \kappa_0$  at each station.  $\Delta \kappa_0$  is the difference between surface and borehole  $\kappa_0$  estimated from empirical regressions on as-recorded horizontal components. The error bar (within-station variability) represents ±1 standard derivation of  $\Delta \kappa(\theta)$  at each station. The horizontal solid line presents the mean of  $\Delta \kappa(\theta)$  across all stations, and the

<sup>&</sup>lt;sup>†</sup>H<sub>800</sub>: depth to a horizon with velocity V<sub>s</sub> of 800 m/s or more

 $<sup>^{\</sup>dagger\dagger}V_{s,mean}$ : the time-averaged shear-wave velocity of the subsoil between surface and borehole sensors

 $<sup>{}^{\</sup>S}\sigma(\Delta\kappa(\theta))$ : standard derivation of  $\Delta\kappa(\theta)$ , which is computed with Equation (5)

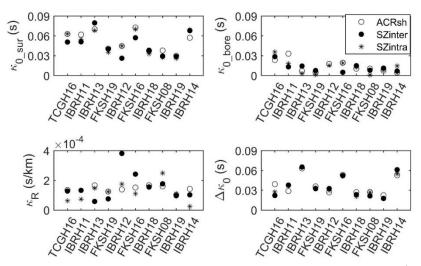
mean( $\Delta \kappa(\theta)$ ): mean of  $\Delta \kappa(\theta)$ , which is computed with Equation (5)

dash lines indicate the  $\pm 1$  standard derivation of  $\Delta \kappa(\theta)$  across all considered stations (between-station variability).

#### 5.2. Earthquake type and focal depth effects on $\kappa_r$ , $\kappa_R$ , and $\kappa_0$ estimations

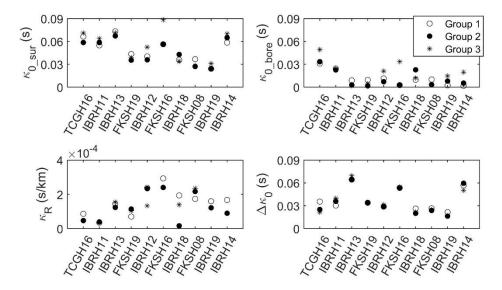
In this section, we investigate the influence of earthquake type and focal depth on average  $\kappa_{r\_AS}$  from as-recorded components, regional attenuation, as captured by  $\kappa_R$ , and  $\kappa_0$  estimations. The algorithm proposed by Garcia et al. (2012) is used herein to classify earthquake types as: (1) shallow active crustal, ACRsh (if the hypocentral depth is less than 35 km), (2) deep active crustal, ACRde (if the hypocentral depth is larger than 35 km), (3) subduction zone intraslab, SZintra (with minimum focal depth of 15 km), and (4) subduction zone interface, SZinter, earthquakes (with minimum focal depth of 70 km).

Values of  $\Delta \kappa_0$ ,  $\kappa_0$  sur,  $\kappa_0$  bore, and  $\kappa_R$  at the selected ten stations are computed for different datasets categorized by earthquake type, and shown in Figure 9. It should be noted that the limited number of ACRde events did not allow for the derivation of the corresponding  $\kappa_0$  and  $\kappa_R$  for this particular dataset. A few negative values of  $\kappa_R$  and  $\kappa_0$  values are obtained at some stations for some of the datasets, which could be caused by the lack of available events for each earthquake type at specific epicentral distance ranges. For example, ACRsh events recorded at IBRH11 only have epicentral distances in the range of 50 to 150 km. Hence, those cases were not included in Figure 9. The resulting  $\kappa_0$  and  $\kappa_R$  values demonstrate that different seismicity types lead to varying estimates of the  $\kappa_R$  component (i.e., the slope of  $\kappa_0$ -model), which in turn affects the estimated site-specific  $\kappa_0$ component (i.e., the intersect in the y-axis at zero epicentral distance). Records from subduction and active crustal earthquakes will be affected by different wave propagation paths, which is reflected in the variability in the path-component  $\kappa_R$ . Variations in  $\Delta \kappa_0$  values at selected stations are relatively small for the different datasets considered, which supports previous research indicating the site-specific nature of  $\Delta \kappa_0$  values that is not affected by the focal depth (i.e., the difference between  $\kappa_0$  sur and  $\kappa_0$  bore represents the seismic attenuation taking place throughout the local soil column, Cabas et al. 2017).



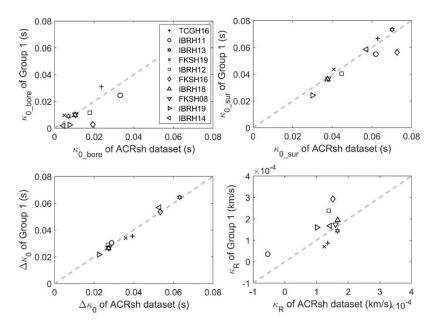
**Figure 9.** Comparisons of  $\kappa_0$  (at the ground surface and at depth),  $\kappa_R$ , and  $\Delta \kappa_0$  values for different earthquake types at each station.

The influence of focal depth on the estimations of  $\kappa_0$  and  $\kappa_R$  is investigated by separating into three groups with focal depths of: (1) less than 35 km (which includes both ACRsh and SZintra events), (2) from 35 km to 70 km (which includes the ACRde and SZintra events), and (3) more than 70 km (which includes the ACRde and SZinter events). A correlation between  $\kappa_R$  values and focal depth is not observed, but  $\kappa_R$  values show less variation when grouped by focal depth (regardless of earthquake type) than by earthquake type as seen in **Figure 10**.



**Figure 10.** Comparisons of  $\kappa_0$  (at the ground surface and at depth),  $\kappa_R$ , and  $\Delta\kappa_0$  (the difference between surface and borehole  $\kappa_0$ ) values for different focal depth groups at each station. Groups 1, 2 and 3 consider focal depths of less than 35 km, from 35 to 70 km, and more than 70 km, respectively.

The influence of earthquake type and focal depth is further explored in **Figure 11**, where  $\kappa_R$ ,  $\kappa_0$  and  $\Delta\kappa_0$  values estimated only using ACRsh events, and a dataset of records with focal depth less than 35 km (i.e., Group 1) are compared. It should be noted that a negative  $\kappa_R$  value is derived at IBRH11 for the ACRsh datasets, which may be caused by the absence of events for epicentral distance less than 50 km. The average differences of  $\kappa_R$  estimations between these two data sets across the ten stations is 28.43% (neglecting the values at IBRH11), while the corresponding average differences of  $\kappa_{0\_sur}$  and  $\Delta\kappa_0$  are 8.77% and 4.51%, respectively. The differences in  $\kappa_R$   $\kappa_{0\_sur}$ ,  $\kappa_{0\_bore}$ , and  $\Delta\kappa_0$  estimates are acceptable, which supports the incorporation of shallow subduction zone events to a shallow crustal event dataset.



**Figure 11.** Comparisons of  $\kappa_0$  (at the ground surface and at depth),  $\kappa_R$ , and  $\Delta\kappa_0$  (the difference between surface and borehole  $\kappa_0$ ) values estimated with ACRsh dataset, and Group 1. Group 1 includes the events with focal depth less than 35 km (which includes both ACRsh and SZintra events).

#### 6. Conclusions

Repeatable contributions from path and site terms to the within-station variability in individual estimates of  $\kappa_r$  and site-specific  $\kappa_0$  were investigated using ten stations from the KiK-net database. Our dataset consisted of linear ground motions with surface PGA less than 0.01 g,  $M_w$  larger than 4.0 and epicentral distance less than 150 km. Both active crustal and subduction earthquakes were used in this work to investigate repeatable contributions from the wave propagation path. Systematic variability on  $\kappa_r$  and  $\kappa_0$  values stemming from the dataset choice, namely the selection of events based on their focal depth and type of seismicity was evaluated. Contributions to the within-station variability associated with ground motion directionality were also investigated.

The influence of ground motion directionality on the estimates of  $\kappa_{r\_AS}$  was studied, and findings from this work revealed that the orientation of ground motion affects estimates of  $\kappa_{r\_AS}$  computed on single horizontal components. However, this influence can be removed when calculating the average of two as-recorded horizontal component  $\kappa_{r\_AS}$  values. Thus, using the mean of two horizontal  $\kappa_{r\_AS}$  values (without considerations of the difference between these two values) is recommended as the representative  $\kappa$  value for each ground motion pair. This is different from previous recommendations to only report  $\kappa_{r\_AS}$  values for which differences between the recorded horizontal components is less than 20%. It was also found that the within-station variability in  $\Delta\kappa_0$  values (i.e., the difference between  $\kappa_0$  values at the surface and at depth) associated with directionality effects can be comparable to the between-station variability. This observation highlights the importance of quantifying the within-station variability on  $\kappa$  estimates in a more robust manner. Moreover, our findings support previous research efforts indicating that site

amplification effects on  $\kappa$  estimates should be minimized in order to obtain reliable estimates at sites of interest. Systematic contributions from event-azimuths were not observed, while the variability in  $\Delta \kappa(\theta)$  estimates with rotation angle was found to be a function of local soil conditions. The influence of ground motion directionality on the parameterization of near-surface attenuation was found to be station-dependent, but further investigation is required to identify relevant correlations between observed ground motion directionality and site properties. Nearsurface seismic attenuation anisotropy could help explain observed variations of  $\Delta \kappa(\theta)$  with ground motion orientation. Anisotropy in Q values has been observed from both laboratory experiments (Tao and King, 1990, Kern et al. 1997) and the analysis of earthquake ground motions (Liu et al. 2005). The random distributed cracks near surface could also cause seismic anisotropy (Liu et al. 1993, Liu et al. 2004, Boness and Zoback 2004), which could then influence seismic wave scattering and reflection. The specific geological condition and volcanic environment in Japan also lead to anisotropy in Q (Pei et al. 2009, and Nakano et al. 2015). More generally, a preferred direction of ground motion independent from the expected polarization (based on focal mechanism and location of the events) has also been observed in recorded data from the Whittier Narrows and Loma Prieta earthquakes (Bonamassa et al. 1991, Bonamassa and Vidale 1991). More research on directionality effects is required to elucidate the physical basis for the observed variation of attenuation characteristics of ground motions with orientation.

Different earthquake types were found to lead to different  $\kappa_R$  values. However, it is important to note that the classification of seismicity type is also tied to the focal depth. Selecting a dataset with considerations of systematic variations stemming from varying focal depths and earthquake types is recommended to resolved  $\kappa$ 's path-component,  $\kappa_R$  more reliably. Deep earthquakes can produce multi-wave propagation paths to the site of interest, which could have a more significant influence on  $\kappa_R$ . On the other hand, the incidence angle of seismic waves when the focal depth is shallow could introduce larger within-station variability. Smaller differences in surface and borehole  $\kappa_0$  values were observed across the datasets used (i.e., different focal depths and/or earthquake types). The lack of variability of  $\Delta\kappa_0$  values as a function of source and path effects evidences that  $\Delta\kappa_0$  is mainly a function of near-surface attenuation, which supports its site-specific nature also observed in previous research studies.

#### 7. Data and Resources

Accelerograms and geotechnical data are obtained from the KiK-net network at http://www.kyoshin.bosai.go.jp (last accessed December 2018), collected and distributed by National Research Institute for Earth Science and Disaster Prevention (NIED). The orientations of borehole sensors are available at <a href="http://www.hinet.bosai.go.jp/st\_info/detail/?LANG=ja">http://www.hinet.bosai.go.jp/st\_info/detail/?LANG=ja</a> (last accessed December 2018). The earthquake information is available F-net network at <a href="http://www.fnet.bosai.go.jp/top.php">http://www.fnet.bosai.go.jp/top.php</a> (last accessed December 2018).

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# Part II: Quantifying the High-frequency Spectral Decay Parameter Kappa (κ) Beyond the Linear-elastic Regime

#### 1. Introduction

The anelastic attenuation of seismic waves as they travel through sedimentary deposits is a function of the deformations induced, which in turn depends on the material properties (e.g., plasticity of the soil) and the intensity of the ground shaking. Material damping ratio,  $\xi$ , is commonly used in geotechnical earthquake engineering to quantify viscous and anelastic energy dissipation in soils subjected to dynamic loading. Empirical models of  $\xi$  often have a constant minimum value (known as minimum shear-strain damping,  $\xi_{min}$ ) for small shear strains considered in the linear-elastic regime (e.g., Darendeli, 2001). Yet values of  $\xi$  increase as larger shear strains are induced in soil deposits by stronger ground excitations (Idriss et al. 1978, Seed et al. 1986, Darendeli 2001). The characterization of  $\xi$  across a wide range of strains is essential to model the effects of local soil conditions on earthquake ground motions.

The high-frequency spectral decay parameter,  $\kappa$  (Anderson and Hough 1984) is based on characteristics of low-intensity ground motions recorded directly in the field, which makes it an observable parameter that quantifies total attenuation (e.g., energy dissipation caused by scattering and anelasticity). Estimates of  $\kappa$  have proven useful in multiple applications, from stochastic modeling of ground motions (Boore 2003) to the development of host-to-target adjustments of ground motion models (e.g., Campbell 2003, Al Atik et al. 2014). The site-specific, distance-independent component of  $\kappa$ , known as  $\kappa_0$  (Anderson 1991) is defined as a site parameter that captures the attenuation due to the propagation of seismic waves through near-surface materials. The relationship between  $\kappa_0$  and  $\xi_{min}$  has been investigated in previous studies (e.g., Cabas et al. 2017; Ktenidou et al. 2015; Zalachoris and Rathje 2015) for weak motion data, but the quantification of  $\kappa$  and  $\kappa_0$  beyond the linear-elastic regime remains unsolved.

Most studies on individual estimates of  $\kappa$ , hereafter referred to as  $\kappa_r$ , and its site-specific component  $\kappa_0$  have used ground motion records that do not trigger nonlinear behavior at the sites of interest (e.g., Van Houtte et al. 2011, Laurendeau et al. 2013, Edwards et al. 2015, Perron et al. 2017). This practice is consistent with the concept of  $\kappa_r$  introduced by Anderson and Hough (1984), who associated the deviation from a flat high-frequency acceleration spectrum to attenuation along the path. However, nonlinear soil behavior has often been responsible for increasing the damage potential of strong ground motions in past earthquakes (e.g., Darragh and Shakal, 1991, Trifunac and Todorovska, 1994, Bonilla et al., 2011, Rong et al., 2016). Understanding near-surface attenuation effects in the nonlinear regime is then necessary for a thorough assessment of seismic hazards and risks imposed to civil infrastructure (Anderson and Hough 1984). Hence, this paper investigates the relationships among  $\kappa$ , shear strains and ground motion intensity to understand the behavior of  $\kappa$  at the onset of nonlinear soil behavior.

#### 2. Background

The first paper that attempted to connect soils' nonlinear response and  $\kappa_r$  was conducted by Yu et al. (1992), where the authors compared two simulated records; one from a linear site response analysis, and the other from a time-domain nonlinear site response analysis. Yu et al. (1992) indicated that the value of  $\kappa_r$  estimated with the Anderson and Hough (1984) approach and corresponding to the motion affected by soil nonlinearity was smaller due to the nonlinear site amplifications at high frequencies. However, later studies found a positive correlation between  $\kappa_r$  (and  $\kappa_0$ ), strain amplitudes and the intensity of ground shaking (e.g., Durward et al 1996; Lacave-Lachet et al 2000; Dimitriu et al. 2001; Van Houtte et al 2014).

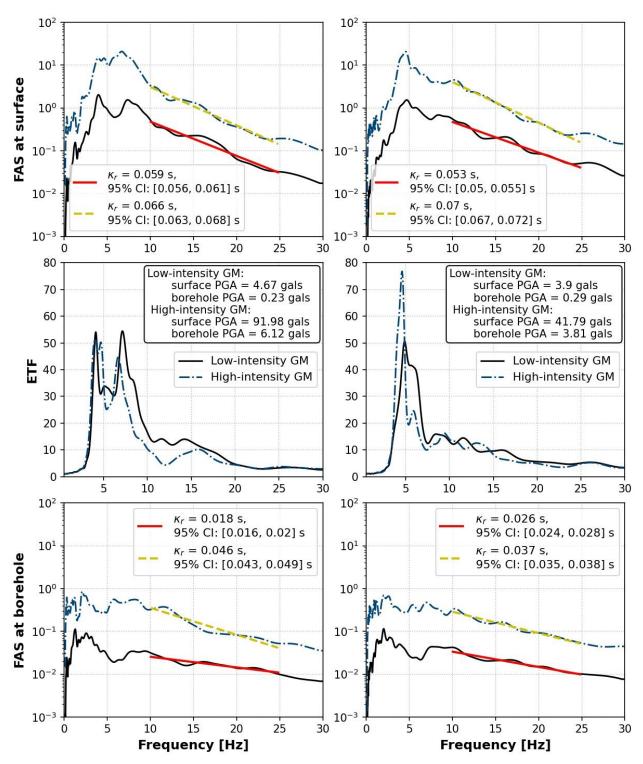
Durward et al. (1996) found that  $\kappa_r$  values were a function of peak ground velocity (PGV, varying from 1 to 100 cm/s), which was used as a proxy for deformation. Values of  $\kappa_r$  were computed for more than 60 records observed at 23 sites in the Imperial Valley, California based on the acceleration spectrum approach (Anderson and Hough, 1984). Durward et al. (1996) hypothesized that soil nonlinearity had affected  $\kappa_r$  because higher  $\kappa_r$  values correlated well with higher PGVs. Moreover, Lacave-Lachet et al. (2000) analyzed ground motions from the 1995 Kobe earthquake in Japan (i.e., the main shock and aftershocks), and found that  $\kappa_r$  values increased with increasing peak ground acceleration (PGA). Hence, Lacave-Lachet et al. (2000) proposed to use  $\kappa_r$  to detect the onset of soil nonlinearity. Dimitriu et al. (2001) investigated the dependency between sitespecific  $\kappa_0$  and ground shaking intensity. Values of  $\kappa_r$  for 23 ground motions (i.e., 46 horizontal components with values of  $\kappa_r$  reported for each individual component) were computed at two adjacent sites in Lefkas, western Greece, based on the acceleration spectrum method. Dimitriu et al. (2001) provided evidence that  $\kappa_0$  was a proxy for soil nonlinearity based on the observed dependency between  $\kappa_0$  and ground shaking amplitudes, which were represented by mean horizontal acceleration in the S-wave window (MGA), PGA, and PGV. Positive correlations were found between the 46 κ<sub>0</sub> values and MGA, PGA, and PGV in log-scale, while a negative correlation was observed between  $\kappa_0$  and the site dominant-resonance frequency. Similarly, Van Houtte et al. (2014) identified a positive correlation between estimates of  $\kappa_0$  and PGA at soft sites using ground motions from the 2010-2011 Canterbury earthquake sequence in New Zealand.

There are still few and contradicting observations of the effects of nonlinearity on  $\kappa_r$  and  $\kappa_0$  estimates (Ktenidou et al. 2015). Additionally, previous studies only considered a very limited database of ground motions. This paper takes advantage of the unique Japanese Kiban-Kyoshin network (KiK-net), which is rich in high-quality ground motions, to further investigate the effects of soil nonlinearity on  $\kappa_r$  and  $\kappa_0$ . More specifically, we explore the dependence of  $\kappa_r$  and  $\kappa_0$  on ground shaking intensity (i.e., weak, moderate or strong ground motions) as parameterized by PGA, and on the level of shear strains induced in near-surface materials at 20 KiK-net stations. First, we present the conceptual basis for the relationship between  $\kappa$ , shear strains and ground motion intensity. Then, we describe our database and methods, starting with the identification of an appropriate classification scheme for linear and nonlinear regimes. The analysis of the effects of ground shaking amplitudes on  $\kappa_r$  at each study site follows. Lastly, we compare the ratio of nonlinear and linear site-specific  $\kappa_0$  across all selected stations to assess the variation of near-surface attenuation estimates from the linear-elastic to the nonlinear regime.

#### 3. Conceptual basis for the interpretation of $\kappa$ beyond the linear-elastic regime

The induced strain level in a given soil layer is a function of the material properties, and the amplitude and frequency content of the incoming wavefield at the site. Stronger ground shaking results in larger-strain responses, which produce an increase in material damping ratio (in combination with a reduction of shear modulus). The short wavelength of high frequency waves allows for multiple cycles of shearing in near-surface sedimentary layers, which makes them more sensitive to the effects of a higher material damping ratio. Thus, we hypothesize that stronger ground shaking inducing larger deformations in sedimentary deposits will affect estimates of the high-frequency spectral decay parameter  $\kappa$ .

Figure 1 provides the acceleration Fourier amplitude spectrum (FAS) and empirical transfer function (ETF) corresponding to a pair of ground motions recorded at depth and at the ground surface at AICH17. One of the ground motion pairs has a low ground shaking intensity (with a surface PGA of less than 5 gals), while the other one has a higher ground shaking intensity (with a surface PGA greater than 40 gals). Computed FAS and ETF are provided for each horizontal component of the low- and high-intensity ground motion pairs in Figure 1. Individual  $\kappa_r$  values are provided for both pairs to explore the validity of our hypothesis with respect to changes in κ due to the intensity of ground shaking. To minimize the bias from path effects and isolate local site effects on individual  $\kappa_r$  values, the selected weak and strong ground motions correspond to events with similar focal depths, azimuths and epicentral distances (i.e., the focal depths, azimuths and epicentral distances are 5 km, 349.2°, and 76.77 km, respectively for the low-intensity event, and 5 km, 350.5°, and 76.95 km, respectively for the high-intensity event). The moment magnitudes of the events associated with the weak and strong ground motions in Figure 1 are 4.2 and 5.2, respectively. To reduce the variability associated with the calculation of  $\kappa_r$  from the acceleration spectrum method, we use the same frequency window for all ground motions (Edwards et al. 2011). Larger values of  $\kappa_r$  at the ground surface (i.e., 0.066 s for horizontal component H<sub>1</sub> and 0.070 s for horizontal component H<sub>2</sub>) are obtained for the high-intensity ground motion compared to the corresponding  $\kappa_r$  values for the low-intensity ground motion (i.e., 0.059 s and 0.053 s for H<sub>1</sub> and H<sub>2</sub>, respectively). The surface PGA values for the low-intensity record are 4.67 and 3.9 gals for H<sub>1</sub> and H<sub>2</sub>, and for the high-intensity ground motion are 91.98 and 41.79 gals. Meanwhile, the ETF corresponding to the high-intensity event shows lower amplifications at higher frequencies (e.g., amplification of varies from 4.3 to 10.6 between 10 and 20 Hz for H<sub>1</sub>) than its counterpart for the low-intensity ground motion (i.e., amplification varies from 4.8 to 17 between 10 and 20 Hz for H<sub>1</sub>), which reflects the stronger influence of increased material damping ratio on high frequencies.



**Figure 1**. Comparisons between a weak and a strong ground motion recorded at AICH17 ( $V_{s30} = 314 \text{ m/s}$ ). The  $M_w$  and  $R_e$  are 4.2 and 76.77 km for the low-intensity ground motion, while 5.2 and 76.95 km for the high-intensity ground motion. The frequency window (i.e., [10, 25] Hz) applied in this plot are picked manually. The left and right columns correspond to analyses conducted on the horizontal components  $H_1$  and  $H_2$ , respectively.

#### 4. Database description

In this study, we use ground motions from the KiK-net database, which provides high quality strong ground motions recorded at more than 600 stations installed uniformly across Japan. Each station possesses a pair of sensors, one at the surface and another one at depth that is typically between 100 to 200 m deep. The sampling frequency of the observed acceleration series is either 100 or 200 Hz. The P- and S-wave velocity profiles are measured by downhole PS logging and available at the KiK-net website (see Resources and Data). The earthquake information, including the seismic moment magnitude  $M_w$ , focal depth and epicenter location are provided by the broadband seismography network (F-net) catalog. The ground motions and flatfile used in this work are processed with the automated protocol proposed by Bahrampouri et al. (2020).

We use surface and borehole horizontal records in this paper. The criteria applied to select records are as follows: (1) epicentral distance is less than 150 km, (2) the SNR ratio is larger than 3.0 at each frequency from 1.0 to 30 Hz, (3) focal depth is less than 35 km (Ji et al. 2020), and (4) the seismic wave path does not pass the Japanese volcanic belt (Nakano et al. 2015). Thus, twenty stations with more than five nonlinear ground motions (the definition of nonlinear ground motions is described next in the Methods section) are used in this work (with 18 stations having more than 10 nonlinear records and 8 stations having more than 15 nonlinear records, see Table 1). Table 1 provides local soil conditions and number of ground motions at each selected site and Figure 2 shows the corresponding locations of selected stations.

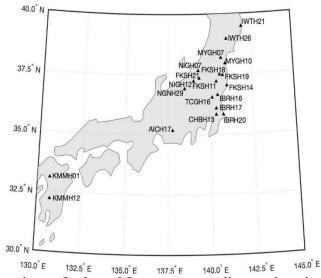
**Table 1.** Local soil conditions, number of ground motions per dataset, predetermined fixed-frequency bandwidth and thresholds for shear strain index,  $I_{\gamma}$  at all study sites.

Station	V <sub>s30</sub> <sup>1</sup> (m/s)	$V_{s0}^2$ (m/s)	V <sub>s,depth</sub> <sup>3</sup> (m/s)	Hole Depth (m)	Number of linear records	Number of transitional records	Number of nonlinear records	$f_{I}^{4}$ (Hz)	f <sub>2</sub> <sup>5</sup> (Hz)	Ι <sub>γ,0,1</sub> <sup>6</sup> (%)	Ι <sub>γ,0,t</sub> <sup>7</sup> (%)
AICH17	314	150	2200	101	23	27	12	12.65	25.00	0.001	0.003
CHBH13	235	220	2920	1300	139	49	11	8.95	25.00	0.001	0.003
FKSH11	240	110	700	115	148	140	26	13.97	25.00	0.001	0.003
FKSH14	237	120	1210	147	114	221	28	10.05	25.00	0.001	0.007
FKSH18	307	140	2250	100	158	103	16	8.95	25.00	0.001	0.003
FKSH19	338	170	3060	100	185	95	21	10.05	25.00	0.001	0.003
FKSH21	365	200	1600	200	60	17	8	12.65	25.00	0.001	0.003
IBRH16	626	140	2050	300	137	81	15	10.05	25.00	0.001	0.003
IBRH17	301	90	2300	510	117	177	18	13.01	25.00	0.001	0.007
IBRH20	244	180	1200	923	133	86	11	8.95	25.00	0.001	0.007
IWTH21	521	150	2460	100	39	24	6	7.38	25.00	0.001	0.003
IWTH26	371	130	680	108	79	32	11	14.24	25.00	0.001	0.003
KMMH01	575	150	1900	100	94	24	15	13.97	25.00	0.001	0.003
KMMH12	410	210	1000	123	134	34	11	11.44	25.00	0.001	0.003
MYGH07	366	130	740	142	59	39	11	12.06	25.00	0.001	0.003

MYGH10	348	110	770	205	229	132	16	14.93	25.00	0.001	0.007
NGNH29	465	150	1040	110	81	38	16	10.05	25.00	0.001	0.003
NIGH07	528	200	1600	106	29	10	11	10.05	25.00	0.001	0.003
NIGH12	553	240	780	110	29	9	11	12.65	25.00	0.001	0.003
TCGH16	213	80	680	112	112	334	35	11.27	25.00	0.001	0.007

 $<sup>^{1}</sup>$  V<sub>s30</sub>: time averaged shear-wave velocity in the top 30 m of the soil profile

 $<sup>^{7}</sup>I_{v,0,t}$ : the shear-strain index threshold to separate transitional and nonlinear datasets



**Figure 2.** Locations of selected Japanese recording stations in this study.

#### 5. Method

#### 5.1. Identification of the onset of nonlinearity

Identifying ground motions that trigger soil nonlinear behavior is key to evaluate  $\kappa$  estimates beyond the linear-elastic regime empirically. The shear-strain index ( $I_{\gamma} = PGV/V_s$ ), which represents the in-situ deformation, and PGA, which describes the peak amplitude of the ground motion, are commonly used to differentiate linear from nonlinear ground motions. Moreover, the correlation between PGA and  $I_{\gamma}$  has been shown to be an effective proxy to capture in-situ stress-strain relationships. This correlation has been characterized via the classic hyperbolic model, which fits empirical observations (Chandra et al. 2014, Chandra et al. 2015, Guéguen et al. 2018).

 $<sup>{}^{2}</sup>V_{s0}$ : shear-wave at the ground surface

 $<sup>{}^{3}</sup>V_{s,depth}$ : shear-wave velocity at the depth of the borehole sensor

 $<sup>{}^4</sup>f_1$ : the lower frequency limit to estimate individual  $\kappa_r$ 

 $<sup>^5</sup>f_2$ : the upper frequency limit to estimate individual  $\kappa_r$ 

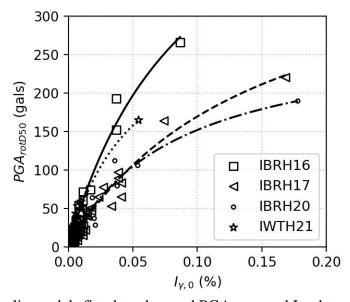
 $<sup>{}^{6}</sup>I_{\gamma,0,l}$ : the shear-strain index threshold to separate linear and transitional datasets

However, there is lack of consensus regarding the sufficiency and efficiency of existing proxies associated with the onset of nonlinear behavior.

We develop appropriate criteria to identify nonlinear ground motions based on examining site response as characterized by both, PGA and  $I_{\gamma}$ . In this paper, the shear-strain index ( $I_{\gamma,0}$ ) at the surface is defined as follows:

$$I_{\gamma,0} = PGV_{rotD50} / V_{s,0} \tag{6}$$

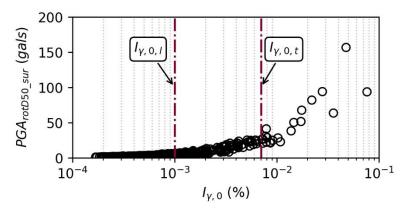
where V<sub>s,0</sub> is the shear-wave velocity at the ground surface, and PGV<sub>rotD50</sub> is the median PGV for all rotated surface ground motions following the approach of Boore (2010). The use of PGV<sub>rotD50</sub> rather than the PGV from recorded ground motion horizontal components can minimize directionality effects. By applying the classic hyperbolic model to describe the correlation between PGA<sub>rotD50</sub> and I<sub>7.0</sub>, we find that there is no unique threshold to identify nonlinear ground motions across all study sites. Figure 3 provides examples of theoretical hyperbolic fitting curves at four stations (i.e., IBRH16, IBRH17, IBRH20 and IWTH21) with varying V<sub>s30</sub> values (from 244 to 626 m/s) to demonstrate the limitations associated with using a single parameter to identify nonlinear ground motions at multiple sites. The scatter points are empirical PGA<sub>rotD50</sub> and I<sub>7,0</sub> pairs from recorded ground motions at the sites of interest, while the lines are the fitting curves from the hyperbolic model. It can be observed that the same deformation at various sites would be triggered by different levels of ground shaking (e.g., I<sub>7.0</sub> of 0.05% will be caused by a PGA<sub>rotD50</sub> around 100 gals at a NEHRP D site, such as IBRH20 with V<sub>s30</sub> of 244 m/s, and by a PGA<sub>rotD50</sub> of 200 gals at a NEHRP C site, such as IBRH16 with V<sub>s30</sub> of 626 m/s). Meanwhile, if nonlinearity is assumed to be triggered when PGA<sub>rotD50</sub> is larger than a predetermined threshold, different levels of I<sub>7.0</sub> will be associated with the onset of soil nonlinearity. Hence, in this work, we propose a hybrid method (further described in the next section) based on both the intensity of the excitation and in-situ deformation to classify ground motions.



**Figure 3.** Hyperbolic models fitted to observed PGA<sub>rotD50</sub> and  $I_{\gamma,0}$  data at four study sites.

#### 5.2. Linear, transitional, and nonlinear datasets

Surface and borehole ground motions are considered separately herein, with borehole records assumed to remain in the linear-elastic regime (i.e., they do not trigger nonlinear behavior at depth). Surface records are separated into three sub-datasets, namely linear, transitional (i.e., soil's behavior is between the linear-elastic and nonlinear regimes), and nonlinear ground motions. First, we define a threshold based on  $I_{\gamma,0}$  to differentiate linear from transitional records, which is hereafter referred to as  $I_{\gamma,0,1}$ . Likewise, a transitional threshold,  $I_{\gamma,0,t}$ , is defined to separate transitional and nonlinear ground motions. The linear  $I_{\gamma,0,1}$  threshold is identified as the onset of soil nonlinearity by visual inspections of the corresponding  $PGA_{rotD50}$  versus  $I_{\gamma,0}$  curve, and corresponds to the point where  $PGA_{rotD50}$  values begin to increase at a higher rate with increasing  $I_{\gamma,0}$ . The transitional  $I_{\gamma,0,t}$  threshold captures when the soil nonlinearity becomes more apparent, which corresponds to the point where the second change in slope of the  $PGA_{rotD50}$  versus  $I_{\gamma,0}$  curve takes place. Figure 4 provides an example of the selection of  $I_{\gamma,0,t}$  and  $I_{\gamma,0,t}$  at station MYGH10. The threshold separating the linear and transitional ground motions is  $I_{\gamma,0,t} = 0.001\%$ , while the threshold separating transitional and nonlinear ground motions is  $I_{\gamma,0,t} = 0.007\%$ .



**Figure 4**. Surface PGA<sub>rotD50</sub> against  $I_{\gamma,0}$  at MYGH10. The red dot-dash lines present the linear and transitional thresholds of  $I_{\gamma,0}$ .

A maximum  $PGA_{rotD50}$  of 25 gals, which is the value adopted by Régnier et al. (2016) to define low-intensity records, is chosen as an additional constraint to avoid linear ground motions being erroneously included into the nonlinear dataset. Thus, linear, transitional, and nonlinear datasets are defined as follows:

- Linear ground motions: records with  $I_{\gamma,0}$  less than the  $I_{\gamma,0,1}$  threshold.
- O Nonlinear ground motions: records with (a)  $I_{\gamma,0}$  larger than the  $I_{\gamma,0,t}$  threshold and (b) PGA<sub>rotD50</sub> larger than 25 gals.
- o Transitional ground motions: records not classified as either linear or nonlinear.

The validity of the proposed linear, transitional, and nonlinear datasets is then tested by examining the behavior of the shear modulus, G against  $I_{\gamma,0}$  at the study sites. The reduction of G for empirical ground motions is estimated as follows (after Guéguen et al., 2019):

$$G/G_{\text{max}} = \frac{PGA_{rotD50}}{PGV_{rotD50}/V_{s,0}} / \left(\frac{PGA_{rotD50}}{PGV_{rotD50}/V_{s,0}}\right)_{\text{max}}$$
(7)

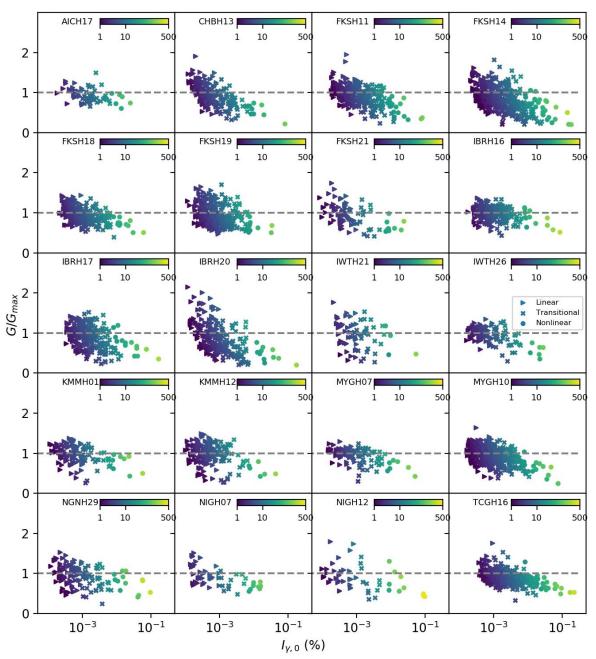
The term 
$$\left(\frac{PGA_{rotD50}}{PGV_{rotD50}/V_{s,0}}\right)_{\text{max}}$$
 is computed from the corresponding average ratio of records with

 $I_{\gamma,0}$  less than 0.001%, which is the predetermined threshold of  $I_{\gamma,0,1}$  for the linear-elastic deformation limit in this work. Figure 5 shows the  $G/G_{max}$  versus  $I_{\gamma,0}$  curves at all study sites. Identified linear ground motions mainly have  $G/G_{max}$  values around 1 ( $G/G_{max}$  values higher than 1 result from using mean G values as a proxy for  $G_{max}$ ), while the ratios corresponding to the nonlinear dataset are generally less than 1 due to the onset of soil nonlinearity. Notably, values of  $G/G_{max}$  associated with the transitional dataset are between the linear and nonlinear datasets. It is not clear whether the site response associated with records identified as transitional could be equivalent to a linear-elastic or a nonlinear response (i.e., associated  $G/G_{max}$  values vary within a single station and across stations). Hence, the characterization as transitional is deemed appropriate.

#### 5.3. $\kappa_r$ AS estimates

We use the acceleration spectrum approach (Anderson and Hough, 1984) to estimate  $\kappa_{r\_AS}$ . To minimize the variability introduced by the selection of the S-wave window, the entire time series is used. Additionally, compatibility with engineering analysis such as geotechnical site response analysis and ground motion models is desired, and such applications use complete time series. Notably, the differences of  $\kappa_{r\_AS}$  values measured from S-wave window and the entire time series are not significant in most cases (Ji et al. 2020).

The variability in estimates of  $\kappa_{r\_AS}$  is a function of the selection of the frequency band (Edwards et al. 2015, Perron et al. 2017) among other factors (Ji et al. 2020, Ktenidou et al. 2013). Moreover, soil nonlinearity affects low and high frequencies differently. The onset of nonlinear soil behavior can influence high frequencies first (Bonilla et al. 2011) because larger shear strains are induced in softer, thinner layers located at shallower depths (i.e., in a profile with increasing stiffness with depth). Hence, we compute  $\kappa_{r,AS}$  based on a pre-determined fixed frequency window ( $[f_1, f_2]$ ). The pre-determined  $f_l$  corresponds to the maximum value between 1.4  $f_c$  (where  $f_c$  is the earthquake source corner frequency of each record) and  $1.4 f_0$  (where  $f_0$  is the site's predominant frequency). If  $f_I$  is lower than  $f_0$ , the value of  $\kappa_{r\_AS}$  will be biased by the site amplification in the high-frequency range (Parolai and Bindi 2004). On the other hand, the  $f_c$  requirement is added to reduce the effects of the earthquake source. The value of  $f_2$  is set to be 25 Hz due to consideration of KiK-net instrument's response (Aoi et al., 2004, Fujiwara et al. 2004, Oth et al. 2011, Laurendeau et al. 2013). The arithmetic average of the resulting  $\kappa_{r\_AS}$  estimated from two orthogonal horizontal components is used (Ji et al. 2020), and negative  $\kappa_{r\_AS}$  values are excluded. These limits ensure a broad frequency bandwidth for  $\kappa$  calculations of at least 10 Hz per record. Additionally, the fixed frequency band reduces potential bias from local amplification effects (Parolai and Bindi, 2004), and minimizes the variability associated with frequency window selections. However, it does not guarantee the most appropriate linear regression for the high-frequency spectral decay, which is the original definition of  $\kappa_r$  by Anderson and Hough (1984). Thus, we further investigate the effects of the frequency band selection for weak and strong ground motion records by comparing the individual  $\kappa_{r\_AS}$  values estimated from a pre-determined fixed frequency window with their counterparts,  $\kappa_{r,auto}$ , resulting from an automated algorithm which does account for the most appropriate linear regression.



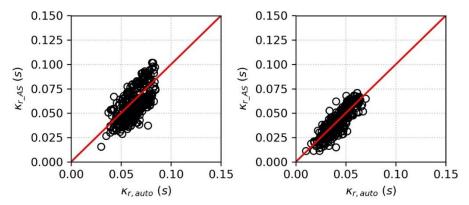
**Figure 5.** G/G<sub>max</sub> versus  $I_{\gamma,0}$  at study sites. The  $G_{max}$  is computed from the average values of  $\left(\frac{PGA_{rotD50}}{PGV_{rotD50}/V_{s,0}}\right)$  of records with  $I_{\gamma,0}$  less than 0.001%. The colors represent PGA<sub>rotD50</sub> values.

The automated procedure used in this paper follows a similar protocol as those presented in Sonnemann, and Halldorsson (2017) and Pilz et al. (2019), which focus on finding the optimal frequency band ( $[f_1, f_2]$ ) to describe the linear decay in the high frequency range. As part of the automated protocol, the minimum  $f_1$  is selected as the maximum value between  $1.5f_0$ , and  $1.5f_c$ . To ensure a minimum frequency bandwidth of 10 Hz, the maximum value of  $f_1$  is 15 Hz and the minimum  $f_2$  corresponds to ( $f_1$ +10) Hz. With 0.5 Hz increments in  $f_1$  and  $f_2$ ,  $f_1$  is varied from the maximum value between  $1.5f_0$  and  $1.5f_c$  to 15 Hz, while  $f_2$  changes from ( $f_1$ +10) Hz to 25 Hz. Going through all the possible combinations of  $f_1$  and  $f_2$ , the frequency range with the minimum root mean square error is set as the optimal frequency band. The errors are computed with the following equation after Pilz et al. (2019):

$$P = \frac{RMS}{\sqrt{\Delta f}}$$
 (8)

Where  $\Delta f$  is the frequency bandwidth, and RMS is the root mean square error between the fitting line and smoothed FAS. The FAS is smoothed with the Konno-Ohmachi filter with a coefficient of 40 (Konno and Ohmachi, 1998). Finally, a visual inspection for the resulting  $\kappa_{r\_AS}$  against epicentral distance plots is conducted to ensure that the  $\kappa_{r,auto}$  values follow the expected linear trend.

Figure 6 compares  $\kappa_{r\_AS}$  and  $\kappa_{r, auto}$  for all selected ground motions at FKSH14. Overall, similar  $\kappa_{r\_AS}$  and  $\kappa_{r, auto}$  estimates are observed, but discrepancies are more significant at the ground surface than at depth. The remaining stations also show an acceptable agreement between the two methods at the surface and at depth. Differences between  $\kappa_{r\_AS}$  and  $\kappa_{r, auto}$  are mainly caused by the complexity of some empirical FAS shapes, for example, when multiple linear decaying trends are present in the high-frequency range.



**Figure 6.** Comparisons of individual  $\kappa_r$  estimates from our automated algorithm,  $\kappa_{r,auto}$ , and the fixed frequency band method,  $\kappa_{r,AS}$  at FKSH14 for surface (left) and borehole (right).

#### 5.4. κ<sub>0</sub>-model

 $\kappa_{r\_AS}$  is generally modeled with contributions from a site-specific component ( $\kappa_0$ ), a path component ( $\kappa_R$ ), and a source component ( $\kappa_s$ ). The source component  $\kappa_s$  is often assumed to be negligible and its contribution is reduced by using a dataset with sufficient records (Van Houtte et

al. 2011, Ktenidou et al. 2014). The linear distance-dependency is commonly applied to capture the path component  $\kappa_R$ , which represents source-to-site effects or regional attenuation (Hough et al. 1988, Anderson, 1991, Ktenidou et al. 2013, Boore and Campbell, 2017). Thus, the most commonly accepted model is described below:

$$\kappa_{r-AS} = \kappa_0 + \kappa_R \times R_e \tag{9}$$

where  $\kappa_0$  and  $\kappa_{r\_AS}$  are in units of time (s),  $\kappa_R$  is in units of second per kilometer (s/km) and  $R_e$  refers to epicentral distance in km. This model is valid when a unique source-to-site path is assumed for each record along with a homogeneous and frequency independent seismic quality factor Q (Knopoff 1964).

The model described by Equation (9) is straightforward to apply when only surface linear ground motion datasets are used. However, the incorporation of nonlinear and borehole ground motions adds complexity to the estimation of regional attenuation as captured by  $\kappa_R$  estimates. In this paper, we assume the regional attenuation to be identical for linear and nonlinear ground motions recorded at the ground surface and at depth. Thus, analogous to the formulation suggested by Douglas et al. (2010) for soil and rock sites, we propose a comprehensive model based on Equation (9), which includes linear and nonlinear surface and borehole records:

$$\kappa_{r\_AS} = N_1 \kappa_{0\_depth} + N_2 \kappa_{0\_lin\_sur} + N_3 \kappa_{0\_nl\_sur} + \kappa_R \times R_e$$
(10)

where  $\kappa_{0\_depth}$  is the site-specific  $\kappa_0$  at depth, and  $\kappa_{0\_lin\_sur}$  and  $\kappa_{0\_nl\_sur}$  are the site-specific linear and nonlinear  $\kappa_0$  at the surface. The coefficients  $N_1$ ,  $N_2$ ,  $N_3$ , and  $N_4$  are defined as follows:

$$N_1 = egin{cases} 1 & for\ dataset\ at\ depth \ 0 & for\ dataset\ at\ the\ surface \end{cases}$$
  $N_2 = egin{cases} 1 & for\ linear\ dataset\ at\ the\ surface \ others \end{cases}$   $N_3 = egin{cases} 1 & for\ nonlinear\ dataset\ at\ the\ surface \ others \end{cases}$ 

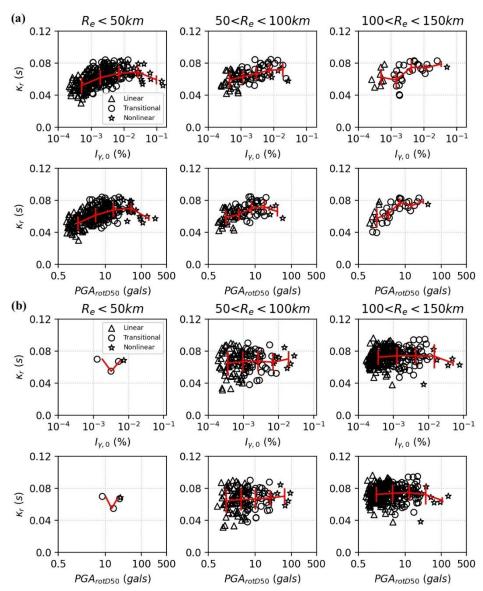
#### 6. Results and Discussion

# 6.1. Effects of soil nonlinearity on empirical $\kappa_{r\_AS}$

First, we study the influence of soil nonlinearity on individual  $\kappa_{r\_AS}$  estimates at each site. As described in Equation (9),  $\kappa_{r\_AS}$  is affected by both local site conditions and path effects in the context of a linear-elastic deformation analysis. To minimize the path component effects as we compare  $\kappa_{r\_AS}$  estimates from multiple events with different ground shaking intensities (captured by differences in PGA<sub>rotD50</sub> and I<sub> $\gamma$ ,0</sub>), we separate all records at each site into three groups based on R<sub>e</sub> (in km). Bins of R<sub>e</sub> considered include [0, 50], [50, 100], and [100, 150]. Within each group,

we assume that the variability from different path contributions is negligible, which allows us to isolate the influence of soil nonlinearity on  $\kappa_{r\_AS}$ .

Figure 7 depicts the correlations among  $\kappa_{r}$  AS, PGA<sub>rotD50</sub> and I<sub>y,0</sub> at FKSH14 (V<sub>s30</sub> = 237 m/s) and MYGH10 ( $V_{s30} = 348$  m/s). It should be noted that we assume that soil nonlinearity is not triggered at depth, and we only study surface records in this section. The triangles, circles, and stars represent the linear, transitional, and nonlinear ground motions, respectively. An overall increasing trend of  $\kappa_{r}$  AS with increasing intensity of ground shaking (either evidenced by increased PGA or  $I_{\gamma,0}$  values) is observed at FKSH14 across the three R<sub>e</sub> groups. Similar trends are observed at other seven study sites with V<sub>s30</sub> less than 400 m/s, which include AICH17, CHBH13, FKSH11, IBRH20, IWTH26, MYGH07, and TCGH16, and at KMMH12 with  $V_{s30}$  greater than 400 m/s. The increasing  $\kappa_r$  AS trend with increasing PGA<sub>rotD50</sub> and I<sub>7,0</sub> is not as significant at MYGH10 though, which has relatively stiffer site conditions compared to FKSH14. Moreover, either no correlation or a slightly decreasing trend is found at other stiff sites with V<sub>s30</sub> greater than 400 m/s (i.e., FKSH21, NIGH12, NGNH29, NIGH07, KMMH01, and IBRH16), and at four softer sites with V<sub>s30</sub> between 300 and 400 m/s (i.e., IWTH21, FKSH18, FKSH19, and IBRH17). We note that the number of available nonlinear records for the R<sub>e</sub> ranges at the sites where the decreasing trend is observed is rather limited. Additional nonlinear records at those sites are necessary (i.e., stronger intensity ground motions) to further evaluate the contributing factors to a potential decreasing trend in  $\kappa_{r}$  AS values. However, in general, we observe that positive correlations between  $\kappa_{r}$  AS and the intensity of ground shaking are more significant at softer sites (e.g., TCGH16 with  $V_{\rm s30}$  of 213 m/s) than at stiffer sites (e.g., KMMH12 with V<sub>s30</sub> of 408 m/s). The data support that the onset of soil nonlinearity can affect  $\kappa_r$  AS estimates, but such influence is station-dependent. The level of soil nonlinearity can be unique at each specific site (for a similar intensity of ground shaking) because of the complexities of the in situ subsurface conditions. We observe the same patterns in our data when using the automated procedure to compute  $\kappa_{r,auto}$ .



**Figure 7**. Correlations between surface  $\kappa_{r\_AS}$  estimates and ground shaking intensities at (a) FKSH14 (V<sub>s30</sub> = 237 m/s) and (b) MYGH10 (V<sub>s30</sub> = 348 m/s). All records are separated into three groups based on the epicentral distance: less than 50 km (left), between 50 and 100 km (middle), and more than 100 km (left). Within each group, records are separated into five bins uniformly, and the vertical red lines are error bars depicting the standard deviation of  $\kappa_{r\_AS}$ . The trend line is presented by connecting mean  $\kappa_{r\_AS}$  values within each bin.

#### 6.2. Effects of soil nonlinearity on the empirical $\kappa_0$ -model

Linear, transitional, and nonlinear ground motion datasets are used in this section to allow the assessment of appropriate values of  $\kappa_0$  beyond the linear-elastic regime. We explore four approaches (i.e., AP1 to AP4) to incorporate records within the transitional dataset into the  $\kappa_0$ -model presented in Equation (5). Table 2 describes how the identified linear, transitional, and nonlinear datasets are used to estimate  $\kappa_0$ \_lin\_sur and  $\kappa_0$ \_nl\_sur. A modified model is also proposed, where the transitional dataset is analyzed independently:

$$\kappa_{r\_AS} = N_1 \kappa_{0\_depth} + N_2 \kappa_{0\_lin\_sur} + N_3 \kappa_{0\_nl\_sur} + N_4 \kappa_{0\_tran\_sur} + \kappa_R \times R_e$$
(11)

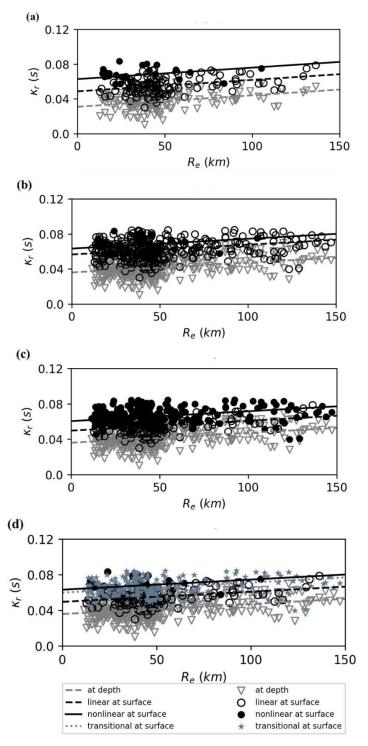
where

$$N_4 = \left\{ egin{matrix} 1 & for \ transitional \ dataset \ at \ surface \ others \end{matrix} 
ight.$$

And  $\kappa_{0\_tran\_sur}$  corresponds to the site-specific  $\kappa_0$  value resulting from the transitional ground motion dataset. Figures 8 and 9 provide the resulting  $\kappa_0$  models from each approach at FKSH14 and MYGH10, respectively. Figure 8 shows that  $\kappa_{r\_AS}$  and  $\kappa_0$  values corresponding to the nonlinear ground motions (regardless of the selected approach to construct the nonlinear dataset) are larger than their linear counterparts at FKSH14. However, results at a stiffer station presented in Figure 9 show little disagreement between  $\kappa_{r\_AS}$  and  $\kappa_0$  values corresponding to the linear and nonlinear motions (regardless of the approach to construct each dataset).

**Table 2.** Ground motion datasets constructed via alternative approaches (AP1 to AP4) explored in this study to implement the  $\kappa_0$ -model.

Approach	K0_lin_sur	K0_nl_sur	K0_tran_sur	K0_depth	κ <sub>0</sub> -model	
AP1	Linear dataset	Nonlinear dataset		Borehole dataset	Equation (5)	
AP2	Linear and transitional datasets	Nonlinear dataset		Borehole dataset	Equation (5)	
AP3	Linear dataset	Nonlinear and transitional datasets		Borehole dataset	Equation (5)	
AP4	Linear dataset	Nonlinear dataset	Transitional datasets	Borehole dataset	Equation (6)	



**Figure 8**. κ<sub>0</sub>-model at FKSH14 from datasets defined by (a) AP1, which only considers the linear and nonlinear datasets, (b) AP2, where transitional records are included as part of the linear dataset, (c) AP3, where transitional records are included as part of the nonlinear dataset, and (d) AP4, where the linear, transitional, and nonlinear datasets are considered separately.

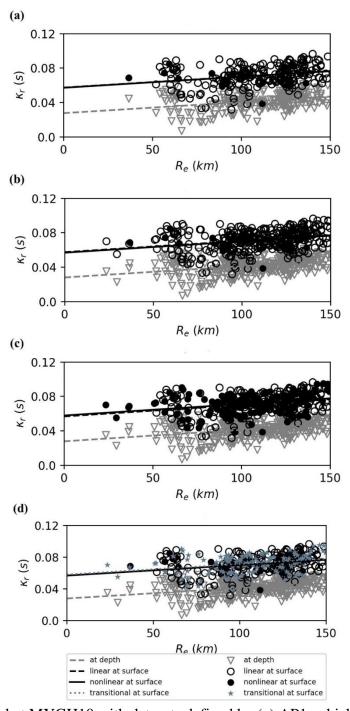
Variations in κ<sub>0\_lin\_sur</sub> estimates are observed as a function of the approach considered to construct the linear datasets (see specific values in Table 3). Similarly, variations in  $\kappa_{0 \text{ nl sur}}$  values are also found across the different approaches to define the nonlinear datasets. At FKSH14 (Figure 8), κ<sub>0 lin sur</sub> estimates are more variable as a function of the dataset definitions (with a maximum difference of 16.16% across approaches AP1 to AP4), compared to  $\kappa_{0 \text{ nl sur}}$  values (with a maximum difference of 4.62%). In addition, Figure 8(d) shows that data points corresponding to the transitional dataset are more compatible with their counterparts within the nonlinear dataset, which may indicate that at FKSH14, the level of nonlinearity induced by the transitional dataset is closer to that induced by the ground motions in the nonlinear dataset. Other study sites such as AICH17 and IWTH21 also show that  $\kappa_{0_{\text{lin\_sur}}}$  estimates are more sensitive to dataset selections. In contrast, variations of  $\kappa_{0\_lin\_sur}$  and  $\kappa_{0\_nl\_sur}$  across datasets at MYGH10 (Figure 9) are small, with maximum differences of only 1.21% and 1.98%, respectively. Large differences in κ<sub>0\_nl\_sur</sub> estimates across datasets are observed at eight sites, but the limited number of nonlinear records at some of those sites (e.g., there are only six nonlinear records at IWTH21, which results in a maximum difference of 47.05% for  $\kappa_{0\_lin\_sur}$  and 11.17% for  $\kappa_{0\_nl\_sur}$ ) may be a contributing factor. Adding transitional records to either the linear or the nonlinear dataset at such sites can significantly bias the regression model. In general, differences in the  $\kappa_0$ -model as a function of the selected dataset are observed in 45% of our study sites (with differences in  $\kappa_0$  lin sur or  $\kappa_0$  nl sur values greater than 10%). This is a relevant observation because it demonstrates the importance of selecting appropriate ground motions even for typical  $\kappa_0$  estimations (i.e., in the linear-elastic regime) at a given site.

**Table 3.** Site-specific  $\kappa_0$  values obtained from different dataset definitions at stations FKSH14 and MYGH10.

	Approach	$\kappa_{0\_lin\_sur}(s)$	$\kappa_{0\_nl\_sur}$ (s)	$\kappa_{0\_tran\_sur}(s)$
	AP1	0.0487	0.0628	
14	AP2	0.0565	0.0633	
FKSH14	AP3	0.0497	0.0605	
	AP4	0.0496	0.0633	0.0600
	Maximum difference	16.16%	4.62%	
	AP1	0.0572	0.0569	
110	AP2	0.0573	0.0567	
MYGH	AP3	0.0566	0.0577	
MY	AP4	0.0567	0.0565	0.0579
	Maximum difference	1.21%	1.98%	

Our findings suggest that the development of a  $\kappa_0$ -model beyond the linear-elastic regime is a function of the definition of what constitutes linear and nonlinear ground motion datasets. The identification of transitional ground motion datasets in this study allows us to assess which records provide estimates of  $\kappa_{r_-AS}$  that are closer to either the linear or the nonlinear behavior at different sites. Differences in behavior triggered by the records within the transitional database may be caused by unique local site conditions (i.e., the level of soil nonlinearity developed at each site) or by limitations of the simplified definition used herein to classify transitional records (i.e., as a

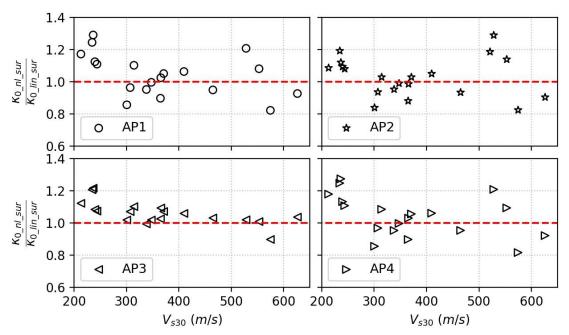
function of PGA and  $I_{\gamma}$ ). Identifying appropriate linear and nonlinear datasets for  $\kappa_{r\_AS}$  estimations requires further research to provide consistent models of near-surface attenuation that can more effectively be implemented from small to large shear strains. However, the site-specific response at each site of interest may lead to challenges in determining appropriate dataset classifications based on a simple, generalized criterion.



**Figure 9**.  $\kappa_0$ -model at MYGH10 with datasets defined by (a) AP1, which only considers the linear and nonlinear datasets, (b) AP2, where transitional records are included as part of the

linear dataset, (c) AP3, where transitional records are included as part of the nonlinear dataset, and (d) AP4, where the linear, transitional, and nonlinear datasets are considered separately.

Figure 10 provides ratios of  $\kappa_{0\_nl\_sur}/\kappa_{0\_lin\_sur}$  at the 20 study sites based on the four different approaches to construct linear and nonlinear datasets (Table 2) explored in this study. Lager ratios are observed at sites with V<sub>s30</sub> lower than 300 m/s regardless of the dataset chosen for the κ<sub>0</sub>model. Differences between  $\kappa_0$  values in the linear and nonlinear regimes seem to be reconciled at sites with higher V<sub>s30</sub> values, where the ratios fluctuate more closely around unity. When grouping intermediate and strong nonlinear ground motions (i.e., AP3), most stations result in ratios of  $\kappa_{0 \text{ nl sur}}/\kappa_{0 \text{ lin sur}}$  larger than one (Figure 10c), which can be interpreted as the signature of soil nonlinearity on the near-surface attenuation estimates (i.e., near-surface attenuation increases with larger deformations as the soil nonlinearity is triggered). When treating linear, transitional, and nonlinear datasets independently (i.e., AP4), there are 12 sites with a ratio larger than one. These findings are consistent with the behavior of material damping ratio observed in dynamic laboratory testing of soils. However, potential bias due to the limited number of nonlinear records in our dataset should not be discarded. For instance, we note a few instances when ratios of  $\kappa_{0 \text{ nl}}$  sur/ $\kappa_{0 \text{ lin}}$  sur are lower than one in Figure 10. Those ratios may result from the limited nonlinear records available at those sites coupled with the uncertainties associated with  $\kappa_{0\_lin\_sur}$  (e.g., Ji et al., 2020). Overall, the variations observed in the  $\kappa_{0\_nl\_sur}/\kappa_{0\_lin\_sur}$  ratio support our hypothesis that soil nonlinearity plays a role on the estimates of near-surface attenuation from recorded ground motions. This effect is station-dependent, and further research is needed to identify the most appropriate parameter or vector of parameters capable of capturing the influence of nonlinear soil behavior on near-surface attenuation. In fact, the weak correlation between V<sub>s30</sub> and the  $\kappa_{0 \text{ nl sur}}/\kappa_{0 \text{ lin sur}}$  ratio evidences the challenges in connecting site conditions and soil nonlinearity via a single site parameter. Multiple parameters that can describe attenuation and impedance effects from the shallow and deep geologic structures should be investigated. Finally, the  $\kappa_{0 \text{ nl sur}}/\kappa_{0 \text{ lin sur}}$  ratio corresponding to IWTH21 ( $V_{s30} = 521 \text{ m/s}$ ) is not shown in Figures 10a, c, and d because it is very large (i.e., approximately 1.8). This observation may result from uncertainties associated with  $\kappa_r$  AS values propagating to estimates of  $\kappa_0$  when the fixed frequency band approach is applied for all records without consideration of the optimal linear decay trend. In fact, the corresponding  $\kappa_{0 \text{ nl sur}}/\kappa_{0 \text{ lin sur}}$  ratio when implementing the automated procedure is approximately 0.90. Finally, to minimize the potential bias caused by the classification of the transitional dataset as either linear or nonlinear in this study, we adopt the AP4 approach (which considers the linear, transitional, and nonlinear datasets independently) to evaluate predictions of near-surface attenuation in the next section of this paper.



**Figure 10.** Ratio of  $\kappa_{0\_nl\_sur}/\kappa_{0\_lin\_sur}$  at selected sites corresponding to the four approaches to define datasets explored in this study.

### 6.3. Effects of soil nonlinearity on predicted near-surface attenuation

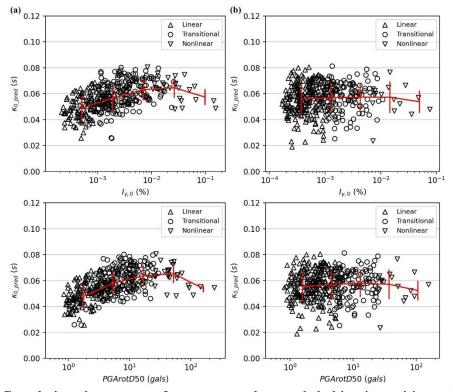
Site-specific  $\kappa_{0\_lin\_sur}$  or  $\kappa_{0\_nl\_sur}$  values from Equation (11) allow for the comparison of empirical estimates of near-surface attenuation in the linear and nonlinear regimes. In this section, we investigate the influence of soil nonlinearity on predictions of near-surface attenuation as captured by  $\kappa_{0\_pred}$ :

$$\kappa_{0 \text{ pred}} = \kappa_{r \text{ AS sur}} - R_e \square \kappa_R \tag{12}$$

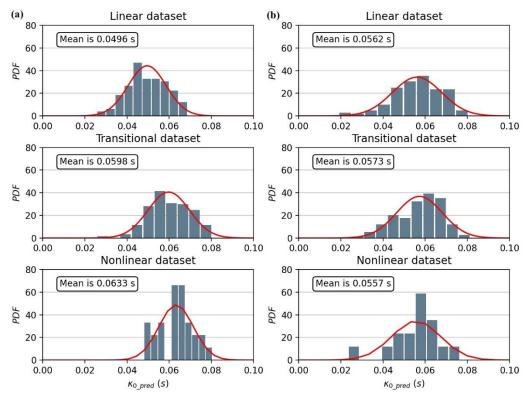
where  $\kappa_{r\_AS\_sur}$  refers to the individual  $\kappa_{r\_AS}$  value for a surface ground motion, and the path-component,  $\kappa_R$ , is based on the values derived with Equation (11) at each site of interest. We assume that by removing the effect of the path-component  $\kappa_R$  from individual  $\kappa_{r\_AS\_sur}$  values, the remaining  $\kappa_{0\_pred}$  is able to provide an approximation to the attenuation contributed by the shallower sedimentary deposits per event. Thus, we can get an estimate of the near-surface attenuation for each observed ground motion at the site of interest.

Figure 11 provides comparisons between  $\kappa_{0\_pred}$  and ground shaking intensity as captured by PGA<sub>rotD50</sub> and I<sub>y,0</sub> at FKSH14 and MYGH10. Values of  $\kappa_{0\_pred}$  first increase and then decrease with increasing PGA<sub>rotD50</sub> and I<sub>y,0</sub> at FKSH14, which are also observed at other six sites (i.e., CHBH13, IBRH20, IWTH26, KMMH12, MYGH07, TCGH16). In contrast, only a weak correlation to the intensity of ground shaking is observed at MYGH10, which further shows that soil nonlinearity effects are not statistically significant at this site for the records selected in this study. Moreover, Figure 12 compares the probability distribution of  $\kappa_{0\_pred}$  values from the linear, transitional, and nonlinear datasets at FKSH14 and MYGH10. The resulting  $\kappa_{0\_pred}$  values are fitted with a Gaussian distribution and the corresponding probability density functions (PDFs) are represented by red

lines. A shift to the right (i.e., toward larger  $\kappa_{0\_pred}$  values) of theoretical PDFs is observed at FKSH14 as ground motions from the linear, transitional, and nonlinear datasets are considered, which are also observed at other four stations (i.e., CHBH13, FKSH11, IBRH20 and TCGH16). The mean  $\kappa_{0\_pred}$  estimates change from 0.0496 s for the linear dataset to 0.0633 s for the nonlinear dataset at FKSH14 (i.e., a difference of 27.6%). In contrast, the variation of mean  $\kappa_{0\_pred}$  between linear and nonlinear datasets at MYGH10 is 0.9%. Generally, an increase and then decrease trend of  $\kappa_{0\_pred}$  estimates from the linear, transitional and nonlinear datasets are observed at eleven sites, and the remaining four sites show a decrease of mean  $\kappa_{0\_pred}$  estimates from linear to transitional motions. Overall, we find that Figures 11 and 12 not only support our hypothesis that the effects of soil nonlinearity on  $\kappa$  are station-dependent, but also show an increasing trend in near-surface attenuation with increasing ground shaking intensity.



**Figure 11.** Correlations between surface  $\kappa_{0\_pred}$  and ground shaking intensities at (a) FKSH14 ( $V_{s30} = 237$  m/s) and (b) MYGH10 ( $V_{s30} = 348$  m/s). At each site, records are separated into five bins uniformly, and the error bars (vertical red lines) show the standard deviation of  $\kappa_{0\_pred}$ . The trend line is presented by connecting mean values of  $\kappa_{0\_pred}$  within each bin.



**Figure 12**. Observed distribution of  $\kappa_{0\_pred}$  at (a) FKSH14 ( $V_{s30} = 237$  m/s) and (b) MYGH10 ( $V_{s30} = 348$  m/s). The red lines present the theoretical probability density function (PDF) fitted with a Gaussian distribution.

# 7. Conclusions

In this work, we investigated the influence of soil nonlinear behavior on individual  $\kappa_{r\_AS}$  and site-specific  $\kappa_0$  estimates at 20 stations selected from the KiK-net database. We also examined the effects of the frequency band selection on  $\kappa_{r\_AS}$  estimates by comparing a predetermined fixed-frequency window approach with an automated procedure, capable of finding the optimal frequency band per record for all records at each site. The selection of a common, fixed and broader frequency band for  $\kappa_{r\_AS}$  estimations reduced the scatter and bias in the data, while providing reasonable estimations of  $\kappa_{r\_AS}$ . Hence, the analyses presented in this paper were conducted with  $\kappa_r$  values estimated by the fixed-frequency band approach.

A consistent identification of ground motions that trigger nonlinear behavior in sedimentary deposits is necessary to quantify near-surface attenuation beyond the linear-elastic regime. Based on the examination of an in-situ stress-strain proxy, namely the correlation between PGArotD50 and  $I_{\gamma,0}$ , we found that variations of shear strains with ground shaking intensity at the onset of nonlinear soil behavior is site-specific. A unique threshold for a single parameter, whether it is PGArotD50 or  $I_{\gamma,0}$ , was not able to capture the onset of soil nonlinearity at our study sites consistently across all sites. Hence, we proposed a hybrid method to classify linear and nonlinear ground motions considering both, PGArotD50 and  $I_{\gamma,0}$ , which resulted in linear, transitional, and nonlinear datasets at each site.

We investigated the influence of soil nonlinearity on  $\kappa_{r\_AS}$  estimates by separating the records into different groups based on epicentral distance to reduce path-component effects. An increasing  $\kappa_{r\_AS}$  trend with increasing PGArotD50 or  $I_{\gamma,0}$  was observed at about half of the study sites. Additionally, we found that  $\kappa_0$  models can be biased by the definition of linear and nonlinear ground motion datasets. Hence, we proposed a  $\kappa_0$  model that minimizes this bias by independently incorporating linear, transitional, and nonlinear records in the  $\kappa_0$  regression. Our results revealed discrepancies between  $\kappa_{0\_lin\_sur}$  (corresponding to the linear-elastic regime) and  $\kappa_{0\_nl\_sur}$  (from the nonlinear regime) at most sites. Such discrepancies were more prevalent among softer sites, and particularly more significant at sites with  $V_{s30}$  less than 300 m/s.

The hypothesis posed and tested in this paper focused on the effects of ground shaking intensity on induced shear strains in sedimentary deposits and associated consequences on the attenuation experienced by seismic waves (particularly in the high frequency range). In general, we find that soil nonlinear behavior can affect estimates of  $\kappa_{r,AS}$  and  $\kappa_0$ , but our results show that this influence is station-dependent. This is reasonable because the wave propagation of short wavelength waves is highly affected by heterogeneities in the soil or rock, local geologic structures, and topography. Further research and strong ground motion data are necessary to identify local site conditions conducive to generate significant changes in near-surface attenuation as captured by  $\kappa_0$  beyond the linear-elastic regime.

#### 8. Data and Resources

Accelerograms and geotechnical data are downloaded from the KiK-net network at http://www.kyoshin.bosai.go.jp (last accessed May 2020). The earthquake information is available from F-net network at http://www.fnet.bosai.go.jp/top.php (last accessed May 2020).

#### 9. Acknowledgements

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# Part III: Estimations of $\kappa_0$ in Low-to-moderate Seismicity Regions

### 1. Introduction

In recent years, the interest in the site-specific high-frequency spectral decay parameter,  $\kappa_0$ , has increased, not only because of its proven advantages when adjusting ground motion prediction models (GMPEs) from host to target regions, and its applications in site-specific PSHA. Values of  $\kappa_0$  can also be used to constrain high frequencies for synthetic or simulated ground motions (e.g., Boore 2003, Cabas et al., 2015; Cabas and Rodriguez-Marek 2017). Additional applications include the use of  $\kappa$  for development of site-specific amplification factors for Ground Motion Response Spectra screening at facilities with limited site characterization data (e.g., EPRI 2013). It has also been shown that the seismic motion on rock and stiff-soil sites does not only depend on the shear wave velocity of near-surface materials, but also on  $\kappa_0$  (Laurendeau et al., 2013).

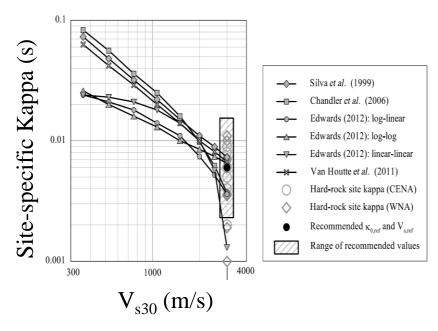
Uncertainty in the estimation of  $\kappa$  is large (Ktenidou et al., 2014), and may have important implications for seismic risk in practice; especially at rock sites, where the estimation of the attenuation or damping in the profile is vital to assessing appropriate levels of high-frequency (> ~5 Hz) design motions. Site attenuation controls the scaling from soft to hard rock at high frequencies (Cotton et al., 2006), as it governs ground motion characteristics in the high-frequency range at short site-source distances, where crustal damping effects are small (Hashash et al., 2014). This is especially relevant for low-attenuating hard rock sites, where the high-frequency components of the ground motion can be underestimated (Perron et al., 2017). Consequently, adjusting the GMPEs to hard-rock conditions is sensitive to  $\kappa_0$  (Ktenidou et al., 2016). For instance, the Pegasos Refinement Project (Biro and Renault 2012) demonstrated how  $\kappa_0$  corrections from soft-rock to hard-rock conditions can lead to differences up to a factor of 3 in the high-frequency part of the response spectrum (Ktenidou et al., 2016).

The objective of this study is to provide recommendations to address the scarcity of records in low-to-moderate seismicity regions and the difficulty in defining their site-specific attenuation models. These efforts will lead naturally into developing more consistent host-to-target adjustments used in site-specific PSHA. Shear wave velocity profiles are more "readily available and well-understood" at local scales, however site-specific  $\kappa_0$  values continue to impose challenges within the PSHA framework. Finally, the convolution of bedrock hazard curves with the site response at the site of interest also requires a consistent treatment of attenuation to avoid double-counting of epistemic uncertainty in the  $\kappa_0$  scaling factors (Ktenidou et al., 2016).

#### 2. Current approaches to estimate $\kappa_0$ for low-to-moderate seismicity regions

Different methodologies to compute  $\kappa$  values or estimate them based on other site parameters such as  $V_{s,30}$  have populated the literature recently (e.g., Silva and Darragh, 1995; Chandler et al. 2006; Drouet et al., 2010; Van Houtte et al., 2011). However, the scatter in  $\kappa_0$ - $V_{s,30}$  relationships is rather large. When it comes to site-specific PSHA, one of the main challenges is the lack of data (particularly events with magnitudes larger than 3), and usable bandwidth (Perron et al., 2017) in low-to-moderate seismicity regions (i.e., target regions), which does not allow the use of the

acceleration spectrum methodology (i.e., Anderson and Hough, 1984 approach, shown in Figure 4b) to compute individual values of  $\kappa$ . The latter is often used for the host regions, which are not usually affected by paucity of records. Consequently, it is critical to understand the differences among the resulting  $\kappa_0$  values from each method before using them in different engineering seismology and earthquake engineering applications, especially in the context site-specific seismic hazard analysis in low-to-moderate seismicity regions. For example, estimates of  $\kappa_0$  for Central and Eastern US (CEUS) have been based on a comprehensive literature review (Hashash et al., 2014) as shown in Figure 1, where an average value of 6±2 ms was selected as representative for the region. Campbell et al., (2013) provides more details on the determination of such value.



**Figure 1.** Estimates of hard-rock  $\kappa_0$  values for CEUS (modified after Hashash et al., 2014)

Ktenidou et al., (2016) explored four approaches (two band-limited and two broadband) for estimating the site  $\kappa_0$  for rock sites in the NGA-East database: the acceleration slope (AS) above the corner frequency, the displacement slope (DS) below the corner frequency, the broadband (BB) fit of the spectrum, and the response spectral shape (RESP) template. These authors found discrepancies among the various methods, and only the broadband methods provided a good agreement with the value provided in the literature for the region (i.e., 6±2 ms). More recent efforts also include the DS, and AS methods to estimate  $\kappa_0$  in mainland France (i.e., Perron et al., 2017). However, all the approaches considered still require the availability of ground motion records.

#### 2.1. Displacement Spectrum Method (Biasi and Smith, 2001)

This is a promising method as it was derived for low-magnitude events and, as indicated by Perron et al., (2017) because "the flatness of the displacement source spectrum below the corner frequency is better understood than the  $\omega^{-2}$  fall-off above the corner frequency" (i.e., the assumption used in the AS method). The method is based on estimating  $\kappa$  from the low-frequency portion of small earthquake displacement spectra. It was introduced by Biasi and Smith (2001), where data from approximately 263 earthquakes with a median magnitude of ML=0.3 were evaluated. One of the

largest sources of uncertainties of this method is the estimation of corner frequencies for the selected events, as they are a function of moment magnitude and stress drop. The latter may not be well constrained for low-to-moderate seismicity regions (Ktenidou et al., 2016).

#### 2.2. Transfer Function Method (Drouet et al., 2010)

Drouet et al. (2010) measured a site-specific (independent of distance)  $\kappa_0$  value directly on the high frequency portion (i.e., frequencies higher than 10 Hz) of a site's transfer function (TF). Source-path-site inversions using weak to moderate earthquakes recorded by the French Accelerometric Network were used to estimate the TF at 76 stations. Kappa values derived from this methodology are called  $\kappa_{0\_TF}$  (Ktenidou et al., 2013). This method quantifies the attenuation of seismic waves taking place between a reference rock horizon and the ground surface. The difference between  $\kappa_{0\_AS}$  (or  $\kappa_{r\_AS}$ ) calculated for bedrock conditions and its counterpart obtained at the ground surface, known as  $\Delta\kappa_{0\_AS}$  (Cabas and Rodriguez-Marek, 2017) has also been proposed as a metric to capture the contribution of sedimentary deposits to overall path attenuation. Thus,  $\kappa_{0\_TF}$  estimates should be theoretically equivalent to  $\Delta\kappa_{0\_AS}$ .

# 2.3. Inverse Random Vibration Theory Method (Al Atik et al., 2014)

This method allows the computation of  $\kappa$ -scaling factors for GMPEs so that high-frequency spectral content can be more robustly characterized. The method is based on inverse random vibration theory as implemented in the computer program Strata (Kottke and Rathje, 2008a,b). A Fourier amplitude spectrum (FAS) is derived such that it is consistent with the response spectrum from the selected GMPE (Al Atik et al., 2014). Then, estimated FAS is scaled from in accordance with the assumed  $\kappa$  values for host and target regions. Finally, Random vibration theory (Cartwright and Longuet-Higgins, 1956) is used to convert the  $\kappa$ -adjusted FAS to response spectrum. This method also provides  $\kappa$ -scaling factors computed as the ratio of the  $\kappa$ -scaled response spectra to the GMPE response spectra (Al ATik et al., 2014).

Previous studies have compared  $\kappa_0$  from Anderson and Hough (1984) with the displacement method (e.g., Ktenidou et al 2016, and Perron et al 2017). The  $\kappa_{DS}$  estimates are believed to better represent material damping in the shallower layers, while the  $\kappa_{AS}$  estimates may reflect a net effect of damping and amplification (Ktenidou et al., 2016). Most recent studies have found  $\kappa$  values from the DS to be larger than the ones obtained from the AS method.

### 3. Comparison between $\Delta \kappa_{0\_AS}$ and $\kappa_{0\_TF}$

### 3.1. Study Sites

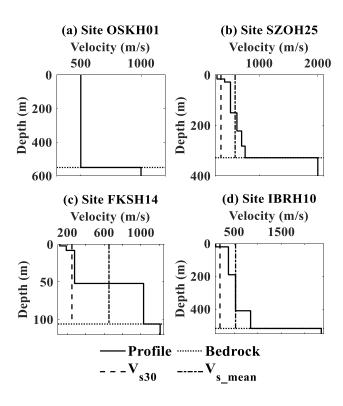
We evaluate four recording stations from the KiK-Net database with an empirical site response that can be represented by a one-dimensional (1D) theoretical linear elastic analysis. Stations FKSH14 and IBRH10 were classified as sites with low inter-event variability and a good fit to 1D theoretical formulations of wave propagation (LG) by Thompson et al. (2012), which make them suitable for linear elastic site response validation analysis. Sites OSKH01 and SZOH25 were not included in the Thompson et al. (2012) study. However, after comparing 1D linear-elastic theoretical and empirical transfer functions at these two sites, they were also deemed suitable for

linear elastic site response validation analysis. While the intent of this research is not to assess the appropriateness of 1D site response models, it is important to select study sites with compatible theoretical and empirical transfer functions. The aforementioned agreement will allow the investigation of the sources of uncertainty in  $\kappa_{0\_TF}$  values to remain independent from the chosen site response model. The  $V_s$  profiles of our study sites are shown in Figure 2.

Site OSKH01 is a single layer site. Site SZOH25 is a multiple–layer site with a smooth  $V_s$  gradient. At FKSH14, there is an impedance contrast (calculated as the ratio between the product of density and  $V_s$  of the overlying layer and the product of the density and  $V_s$  of the underlying layer; hence, the lower the ratio, the stronger the impedance contrast) of 0.24 at 52m depth. At IBRH10, the  $V_s$  gradient is slightly higher than for SZOH25 and the impedance contrast at bedrock is significant (i.e., 0.31). Values of  $V_{s30}$ ,  $V_{s\_mean}$  (time–averaged  $V_s$  for entire depth of soil profile), depth to bedrock and NEHRP (National Earthquake Hazards Reduction Program) site classification (FEMA 450) for each site are provided in Table 1.

Table 1. Selected Site Details and Classification

Site Name	Depth to Bedrock (m)	V <sub>s30</sub> (m/s)	$egin{aligned} \mathbf{V_{s\_mean}} \ (\mathbf{m/s}) \end{aligned}$	NEHRP Site Classification
OSKH01	550	500	500	С
SZOH25	328	347.3	589.1	D
FKSH14	106	251.3	654	D
IBRH10	518	200	531.3	D



**Figure 2.** Shear wave velocity profiles of selected KiK–net sites.

#### 3.2. Ground Motion Selection

We compute  $\kappa_{0\_TF}$  for at least 10 ground motion pairs at each site. We use both horizontal components of the recorded motions and values of  $\kappa_{0\_TF}$  are reported as the average per horizontal component orientation. Each selected record is processed following protocols in Dawood et al. (2016) to comply with signal processing recommendations, such as baseline corrections and adequate noise windows (Ktenidou et al., 2012). The initial selection criteria of processed ground motions is based on peak ground accelerations lower than  $10\text{cm/s}^2$  (to avoid the onset of soil nonlinear behavior), moment magnitudes between 3 and 5, epicentral distances less than 180 km (to avoid bias by multiple seismic ray paths) and shear strain index,  $I_{\gamma}$  (defined as the ratio of peak ground velocity and  $V_{s30}$ ; Chandra et al., 2016) less than 0.1% (to further constrain only linear motions) as shown in Table 2.

The values of  $\kappa_{r\_AS\_bedrock}$ ,  $\kappa_{r\_AS\_surface}$ , and  $\kappa_{0\_TF}$  are evaluated between 10Hz and 25Hz. For further screening, we identify amplification peaks on the empirical transfer functions taking place beyond 8Hz, so that  $\kappa_{r\_AS\_bedrock}$ ,  $\kappa_{r\_AS\_surface}$ , and  $\kappa_{0\_TF}$  are calculated for attenuating slopes not biased by high–frequency amplifications (Parolai and Bindi, 2004). Transfer functions are calculated using smoothed FAS of each horizontal component by applying the Konno–Ohmachi filter (Konno & Ohmachi, 1998). Any recording affected by site amplification peaks beyond 8Hz is rejected from our database (Parolai and Bindi, 2004).

**Table 2.** Initial Ground Motion Screening Criteria

Parameter	Value	Reference
SNR	<3	Ktenidou et al. (2012)
PGA	$<10 \text{cm/s}^2$	Ktenidou et al. (2012)
Magnitude	3-5	Drouet et al. (2010)
<b>Epicentral Distance</b>	<180km	Anderson and Hough (1984)
Shear Strain Index	< 0.1%	Cabas et al. (2017)

# 3.3. Empirical estimations of $\Delta \kappa_{0\_AS}$ and $\kappa_{0\_TF}$

At every site, we estimate site–specific kappa from recorded motions. Since the FAS method is more commonly used, we calculate and compare values of  $\Delta\kappa_{0\_AS}$  and  $\kappa_{0\_TF}$  using the recorded motions at bedrock and at the ground surface. For each recorded motion pair at the study sites,  $\kappa_{r\_AS\_bedrock}$  is evaluated from the spectral decay of acceleration FAS evaluated from the recording observed at the bedrock.  $\kappa_{r\_AS\_surface}$  is calculated from the spectral decay of acceleration FAS of the recording at the surface. Thus, the site–specific kappa estimate,  $\Delta\kappa_{0\_AS}$ , is obtained as follows:

$$\Delta \kappa_{0\_AS} = \kappa_{r\_AS\_surface} - \kappa_{r\_AS\_bedrock}$$
 (1)

Empirical transfer functions (ETF) are calculated as the ratio of the FAS corresponding to the surface ground motion and the FAS corresponding to the ground motion recorded at the downhole sensor depth for each recording pair at the study sites. As proposed by Drouet et al. (2010),  $\kappa_{0}$ \_TF is then calculated as the slope of the decaying peaks in the high-frequency range of

the ETF. We hypothesize that the contribution of the sedimentary deposit to the overall attenuation can be captured by  $\kappa_{0\_TF}$  analogously to the characterization provided by  $\Delta\kappa_{0\_AS}$  (Cabas and Rodriguez-Marek, 2017). Importantly, the same frequency range (i.e.,  $f_1$  and  $f_2$ ) is used to evaluate  $\kappa_{0\_TF}$  from the ETF and the acceleration method for each record.

Tables 3 to 6 provide our resulting empirical site-specific values of  $\kappa$  at each study site. Estimates of  $\kappa_{0\_TF}$  and  $\Delta\kappa_{0\_AS}$  are provided per horizontal component and also as the mean of both horizontal components of selected ground motions. Selected frequency bands per record are also provided and remain the same for both the acceleration and the transfer function method. As a result, we find a very good agreement among estimates of site-specific  $\kappa$  values for all study sites. Such observation is very promising, as we further explore the transfer function method as a viable approach to obtain estimates of site-specific  $\kappa$  values in low-to-moderate seismicity regions. Ongoing research by the PI includes the assessment of theoretical TFs from one-dimensional site response models as proxies for ETFs to estimate  $\kappa_{0\_TF}$ .

#### 4. Conclusions

The estimation of site–specific kappa from the acceleration spectrum method ( $\kappa_{0\_AS}$ ) is needed for various engineering design purposes and requires the availability of abundant ground motion data. At low–to–moderate seismicity regions such as Central and Eastern United States, the scarcity of strong ground motion data limits the applicability of  $\kappa_{0\_AS}$ .

In this study, we first examined the equivalency between empirical estimates of  $\Delta\kappa_{0\_AS}$  and  $\kappa_{0\_TF}$ . Based on four sites and a total of 50 records, our study found that the estimates of both  $\Delta\kappa_{0\_AS}$  and  $\kappa_{0\_TF}$  agree if kappa values at bedrock ( $\kappa_{r\_AS\_bedrock}$ ), at the ground surface ( $\kappa_{r\_AS\_surface}$ ) and the ones from the empirical transfer function at the site of interest ( $\kappa_{0\_TF}$ ) are evaluated within the same frequency bands.

Future research will investigate site-specific  $\kappa_{0\_TF}$  from theoretical transfer functions from site response analysis and  $\kappa_{0\_RVT}$  values resulting from inverse random vibration theory (Al Atik et al. 2014), their limitations and similarities to the near-surface attenuation as captured by the  $\kappa_{0}$  values from the traditional acceleration method (Anderson and Hough 1984).

Table 3: Ground Motion Details and Empirical Site-Specific Kappa (in sec) at OSKH01 (single-layer site)

							N	S Direction			EW Direction					
Record Number	Magnitude (Mw)	Epicentral Distance (km)	PGA (g) (NS)	PGA (g) (EW)	f <sub>1</sub> (Hz)	f <sub>2</sub> (Hz)		tion Spectrum - κ <sub>r_AS_Sur_NS</sub> - κ		Transfer Function Method	f <sub>1</sub> (Hz)			Spectrum Metl <sub>S_Sur_EW</sub> - κ <sub>r_AS_1</sub>	hod (Δκ <sub>0_AS_EW</sub> <sub>Bore_EW</sub> )	Transfer Function Method
							$\kappa_{r\_AS\_Bore\_NS}$	κ <sub>r_AS_Sur_NS</sub>	$\Delta \kappa_{0\_AS\_NS}$	$\kappa_{0\_TF\_NS}$			$\kappa_{r\_AS\_Bore\_EW}$	$\kappa_{r\_AS\_Sur\_EW}$	$\Delta\kappa_{0\_AS\_EW}$	$\kappa_{0\_TF\_EW}$
45990	3.9	34.5	0.007	0.007	12.5	22.5	0.0023	0.0327	0.0304	0.0304	15.0	25.0	0.0100	0.0230	0.0130	0.0130
45999	4.0	86.0	0.002	0.003	13.5	25.0	0.0178	0.0583	0.0405	0.0405	15.0	25.0	0.0118	0.0172	0.0054	0.0054
46002	4.3	66.1	0.006	0.010	14.0	24.0	0.0576	0.0743	0.0166	0.0166	14.0	24.0	0.0435	0.0303	-0.0132	-0.0132
46007	4.5	62.4	0.004	0.005	15.0	25.0	0.0153	0.0443	0.0290	0.0290	14.5	25.0	0.0049	0.0180	0.0131	0.0131
62332	3.9	83.8	0.002	0.002	15.0	25.0	0.0348	0.0638	0.0290	0.0290	14.0	25.0	0.0281	0.0321	0.0039	0.0039
62342	4.3	92.1	0.003	0.004	15.0	25.0	0.0455	0.0604	0.0149	0.0149	15.0	25.0	0.0337	0.0265	-0.0071	-0.0071
62345	4.3	84.0	0.002	0.002	14.5	24.5	0.0418	0.0773	0.0356	0.0356	14.0	24.5	0.0289	0.0327	0.0037	0.0037
90554	4.2	56.1	0.002	0.002	10.0	20.0	0.0161	0.0483	0.0322	0.0322	14.5	24.5	0.0368	0.0518	0.0150	0.0150
93053	4.8	58.3	0.005	0.005	10.0	25.0	0.0269	0.0526	0.0257	0.0257	15.0	25.0	0.0221	0.0308	0.0087	0.0087
130642	4.8	98.8	0.006	0.005	10.5	21.5	0.0261	0.0316	0.0055	0.0055	15.0	25.0	0.0241	0.0403	0.0162	0.0162
	•		•	•		$\Delta\kappa_{0}$ _NS_Emp_Mean		0.0260	0.0260	$\Delta \kappa_{0}$ <sub>EW</sub> <sub>Emp</sub> <sub>Mean</sub>			0.0059	0.0059		
						Standard Deviation			0.0100	0.0100			ndard Deviati		0.0092	0.0092

**Table 4:** Ground Motion Details and Empirical Site-Specific Kappa (in sec) at SZOH25 (multi-layer, smooth Vs gradient site, deep impedance contrast)

					NS Direction EW Dir								<b>EW Direction</b>	rection		
Record Number	$\begin{array}{c} \mathbf{Magnitude} \\ (\mathbf{M_w}) \end{array}$	Epicentral Distance (km)	PGA (g) (NS)	PGA (g) (EW)	<b>f</b> <sub>1</sub> ( <b>Hz</b> )	<b>f</b> <sub>2</sub> ( <b>Hz</b> )		tion Spectrum - K <sub>r_AS_Sur_NS</sub> - K		Transfer Function Method	f <sub>1</sub> (Hz)	f <sub>2</sub> (Hz)		tion Spectrum K <sub>r_AS_Sur_EW</sub> - 1		Transfer Function Method
							K <sub>r_AS_Bore_NS</sub>	κ <sub>r_AS_Sur_NS</sub>	$\Delta \kappa_{0\_AS\_NS}$	$\kappa_{0\_TF\_NS}$			κ <sub>r_AS_Bore_EW</sub>	$\kappa_{r\_AS\_Sur\_EW}$	$\Delta\kappa_{0\_AS\_EW}$	$\kappa_{0\_TF\_EW}$
49372	3.6	73.7	0.0003	0.0003	13.0	23.0	-0.0019	0.0525	0.0544	0.0544	10.0	21.5	0.0497	0.0447	-0.0050	-0.0050
49382	4.4	94.5	0.0003	0.0005	13.5	23.5	-0.0096	0.0572	0.0668	0.0668	15.0	25.0	0.0362	0.0704	0.0342	0.0342
49384	3.9	80.8	0.0003	0.0003	14.5	24.5	0.0143	0.0854	0.0711	0.0711	10.5	21.5	0.0376	0.0442	0.0066	0.0066
49387	4.1	69.6	0.0008	0.0008	10.0	20.0	0.0415	0.0521	0.0106	0.0106	15.0	25.0	0.0339	0.0923	0.0584	0.0584
49399	3.6	39.3	0.0005	0.0005	11.5	23.0	-0.0076	0.0586	0.0662	0.0662	14.5	24.5	0.0458	0.0677	0.0219	0.0219
49411	4.0	50.9	0.0004	0.0003	10.0	20.0	0.0442	0.0612	0.0170	0.0170	11.5	22.5	0.0539	0.0524	-0.0015	-0.0015
73026	4.3	136.6	0.0003	0.0004	11.0	22.5	0.0108	0.0554	0.0446	0.0446	15.0	25.0	0.0494	0.0747	0.0253	0.0253
81921	4.1	15.4	0.0011	0.0009	14.5	24.5	0.0095	0.0876	0.0782	0.0782	10.5	20.5	0.0345	0.0385	0.0040	0.0040
87619	3.9	32.7	0.0007	0.0006	11.0	22.0	-0.0066	0.0252	0.0318	0.0318	10.5	20.5	-0.0214	0.0030	0.0244	0.0244
165233	4.4	174.3	0.0004	0.0004	14.5	24.5	0.0259	0.0650	0.0391	0.0391	15.0	25.0	0.0229	0.0507	0.0278	0.0278
	•			•		Δн	O_NS_Emp_Mean		0.0480	0.0480	Δκ <sub>0_EW_Emp_Mean</sub>			0.0196	0.0196	
						Standard Deviation			0.0221	0.0221	Standard Deviation				0.0182	0.0182

**Table 5:** Ground Motion Details and Empirical Site-Specific Kappa (in sec) at FKSH14 (multi-layer, shallow impedance contrast site)

							N	S Direction						EW Direction		
Record Number	Magnitude (M <sub>w</sub> )	Epicentral Distance (km)	PGA (g) (NS)	PGA (g) (EW)	f <sub>1</sub> (Hz)	<b>f</b> <sub>2</sub> ( <b>Hz</b> )		tion Spectrum K <sub>r_AS_Sur_NS</sub> - K		Transfer Function Method	f <sub>1</sub> (Hz)	f <sub>2</sub> (Hz)		tion Spectrum - κ <sub>r_AS_Sur_EW</sub> - ι		Transfer Function Method
							K <sub>r_AS_Bore_NS</sub>	κ <sub>r_AS_Sur_NS</sub>	$\Delta \kappa_{0\_AS\_NS}$	$\kappa_{0\_TF\_NS}$			K <sub>r_AS_Bore_EW</sub>	κ <sub>r_AS_Sur_EW</sub>	$\Delta\kappa_{0\_AS\_EW}$	$\kappa_{0\_TF\_EW}$
9673	4.8	111.3	0.002	0.003	11.5	21.5	0.0477	0.0561	0.0083	0.0083	10.5	20.5	0.0590	0.0785	0.0195	0.0195
64601	4.2	132.0	0.003	0.002	11.0	21.0	0.0477	0.0785	0.0308	0.0308	10.0	20.0	0.0599	0.0941	0.0342	0.0342
89057	4.3	87.1	0.001	0.001	12.5	22.5	0.0367	0.0991	0.0624	0.0624	15.0	25.0	0.0485	0.0355	-0.0130	-0.0130
108184	3.9	16.2	0.006	0.005	13.0	23.0	0.0071	0.0535	0.0464	0.0464	11.5	24.5	0.0180	0.0532	0.0352	0.0352
108226	3.9	19.9	0.007	0.007	15.0	25.0	0.0323	0.0767	0.0444	0.0444	10.0	20.0	0.0649	0.0904	0.0255	0.0255
108229	4.2	31.8	0.002	0.002	10.0	20.0	0.0442	0.0538	0.0096	0.0096	10.0	20.0	0.0412	0.0709	0.0297	0.0297
108235	4.2	25.6	0.002	0.003	12.5	22.5	0.0286	0.0633	0.0347	0.0347	14.0	25.0	0.0282	0.0329	0.0047	0.0047
108256	4.4	62.7	0.003	0.004	12.0	25.0	0.0377	0.0565	0.0188	0.0188	14.5	24.5	0.0411	0.0382	-0.0029	-0.0029
108288	3.9	26.8	0.005	0.004	10.0	21.5	0.0387	0.0414	0.0027	0.0027	15.0	25.0	0.0337	0.0296	-0.0041	-0.0041
117542	4.3	34.2	0.005	0.005	11.0	22.0	0.0322	0.0542	0.0220	0.0220	15.0	25.0	0.0131	0.0178	0.0047	0.0047
117551	3.8	17.8	0.006	0.007	12.5	24.5	0.0137	0.0651	0.0514	0.0514	10.0	21.5	0.0422	0.0659	0.0237	0.0237
117552	4.3	46.8	0.003	0.004	10.0	22.0	0.0422	0.0585	0.0163	0.0163	15.0	25.0	0.0336	0.0288	-0.0048	-0.0048
121976	3.9	52.4	0.002	0.002	10.0	25.0	0.0303	0.0489	0.0186	0.0186	10.0	20.0	0.0376	0.0694	0.0318	0.0318
122006	3.8	112.6	0.001	0.002	12.5	25.0	0.0244	0.0509	0.0265	0.0265	15.0	25.0	0.0307	0.0376	0.0069	0.0069
127503	3.9	55.0	0.001	0.001	12.0	23.5	0.0311	0.0578	0.0267	0.0267	10.0	20.0	0.0298	0.0702	0.0404	0.0404
						$\Delta\kappa_{0\_{ m NS\_Emp\_Mean}}$			0.0280	0.0280	$\Delta\kappa_{0}_{ m EW}_{ m Emp}_{ m Mean}$				0.0154	0.0154
						Standard Deviation			0.0165	0.0165	Standard Deviation				0.0169	0.0169

**Table 6:** Ground Motion Details and Empirical Site-Specific Kappa (in sec) at IBRH10 (multi-layer, higher Vs gradient, deep impedance contrast)

		Epicentral Distance (km)					N N	S Direction	/					EW Direction		
Record Number	Magnitude (M <sub>w</sub> )		PGA (g) (NS)	PGA (g) (EW)	f <sub>1</sub> (Hz)	<b>f</b> <sub>2</sub> ( <b>Hz</b> )		tion Spectrum		Transfer Function Method	f <sub>1</sub> (Hz)	(Hz) <b>f</b> <sub>2</sub> (Hz)		tion Spectrum = κ <sub>r_AS_Sur_EW</sub> - 1		Transfer Function Method
							κ <sub>r_AS_Bore_NS</sub>	K <sub>r_AS_Sur_NS</sub>	$\Delta \kappa_{0\_AS\_NS}$	$\kappa_{0\_{TF\_NS}}$			κ <sub>r_AS_Bore_EW</sub>	κ <sub>r_AS_Sur_EW</sub>	$\Delta\kappa_{0\_AS\_EW}$	$\kappa_{0\_TF\_EW}$
109418	4.2	144.6	0.001	0.001	11.0	21.0	-0.0403	0.0366	0.0769	0.0769	10.5	20.5	-0.0274	0.0457	0.0731	0.0731
109476	4.0	132.1	0.002	0.003	11.0	21.0	-0.0122	0.0666	0.0789	0.0789	10.5	20.5	0.0047	0.0755	0.0707	0.0707
117946	3.9	122.0	0.004	0.006	11.0	21.0	-0.0068	0.0592	0.0661	0.0661	10.5	20.5	0.0086	0.0761	0.0675	0.0675
117948	4.3	97.3	0.003	0.003	11.5	21.5	-0.0070	0.0572	0.0641	0.0641	10.5	20.5	0.0174	0.0846	0.0672	0.0672
122538	4.6	152.6	0.001	0.001	11.0	21.5	-0.0046	0.0701	0.0747	0.0747	10.5	20.5	0.0229	0.0822	0.0592	0.0592
122550	4.2	98.3	0.003	0.003	11.0	21.0	0.0093	0.0675	0.0581	0.0581	10.5	20.5	0.0047	0.0761	0.0715	0.0715
122552	3.9	94.9	0.003	0.003	11.5	21.5	0.0092	0.0736	0.0644	0.0644	11.0	21.0	0.0307	0.1048	0.0741	0.0741
122567	4.0	145.3	0.001	0.001	10.5	20.5	-0.0264	0.0343	0.0607	0.0607	10.5	20.5	-0.0304	0.0594	0.0898	0.0898
122581	4.2	96.5	0.003	0.003	10.5	20.5	-0.0053	0.0392	0.0445	0.0445	10.5	20.5	-0.0153	0.0627	0.0780	0.0780
128032	4.2	97.5	0.004	0.003	10.5	20.5	-0.0317	0.0317	0.0633	0.0633	10.5	20.5	-0.0057	0.0663	0.0720	0.0720
128033	3.8	113.3	0.003	0.002	12.0	22.0	-0.0018	0.0516	0.0534	0.0534	10.5	20.5	-0.0066	0.0759	0.0825	0.0825
128041	4.0	132.6	0.001	0.001	11.0	21.0	-0.0041	0.0515	0.0556	0.0556	10.5	20.5	-0.0090	0.0608	0.0698	0.0698
128042	3.9	104.5	0.002	0.002	11.0	21.5	-0.0184	0.0370	0.0554	0.0554	10.5	20.5	-0.0351	0.0473	0.0824	0.0824
·			•			Δκ <sub>0_NS_Emp_Mean</sub>			0.0628	0.0628	Δκ <sub>0_EW_Emp_Mean</sub>				0.0737	0.0737
						Standard Deviation			0.0095	0.0095	Standard Deviation				0.0076	0.0076

#### 5. Data and Resources

Accelerograms and geotechnical data are downloaded from the KiK-net network at http://www.kyoshin.bosai.go.jp (last accessed August 2020).

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# **Bibliography**

The following publications resulted from this project. One published paper, one under review and at least one more manuscript is currently being prepared for submission to a peer-reviewed journal. Additionally, results from this project are (or will be) presented at professional conferences (resulting in three peer-reviewed conference abstracts by the time this technical report was submitted):

- Ji, C., Cabas, A., Cotton, F., Pilz, M., and Bindi, D. (2020), Within station variability in kappa: evidence of directionality effects. *Bull. Seism. Soc. Am https://doi.org/10.1785/0120190253*
- Ji, C., Cabas, A., Bonilla, L.F., Gelis, C., (2020) Quantifying the High-frequency Spectral Decay Parameter Beyond the Linear-elastic Regime, Bull. Seism. Soc. Am. (under review)
- Ji, C., Cabas, A., Al Atik, L., (2021) Near-surface attenuation estimates for low-to-moderate seismicity regions (in preparation)
- Cabas, A., Ji, C., Bonilla, L.F., Gelis, C., (2021) Kappa and Material Damping: Insights from the Linear and Nonlinear Soil Behavior Regimes, 6th IASPEI / IAEE International Symposium: Effects of Surface Geology on Seismic Motion, Kyoto, Japan, March 15-17, 2021 (extended abstract)
- Ji, C., Cabas, A., Bonilla, L.F., Gelis, C., (2020) Investigation of the correlation between kappa and soil nonlinearity, Oral presentation at the 2020 ES-SSA Annual Meeting [virtual conference] October 14-15, 2020.
- Ji, C., Cabas, A., Bonilla, L.F., Gelis, C., (2020) Does Nonlinear Soil Behavior Affect Kappa Estimates? Poster presentation at the 2020 SSA Annual Meeting, Albuquerque, NM, April 27-30, 2020. [cancelled due to COVID-19] (abstract to be printed in Seismological Research Letters).